

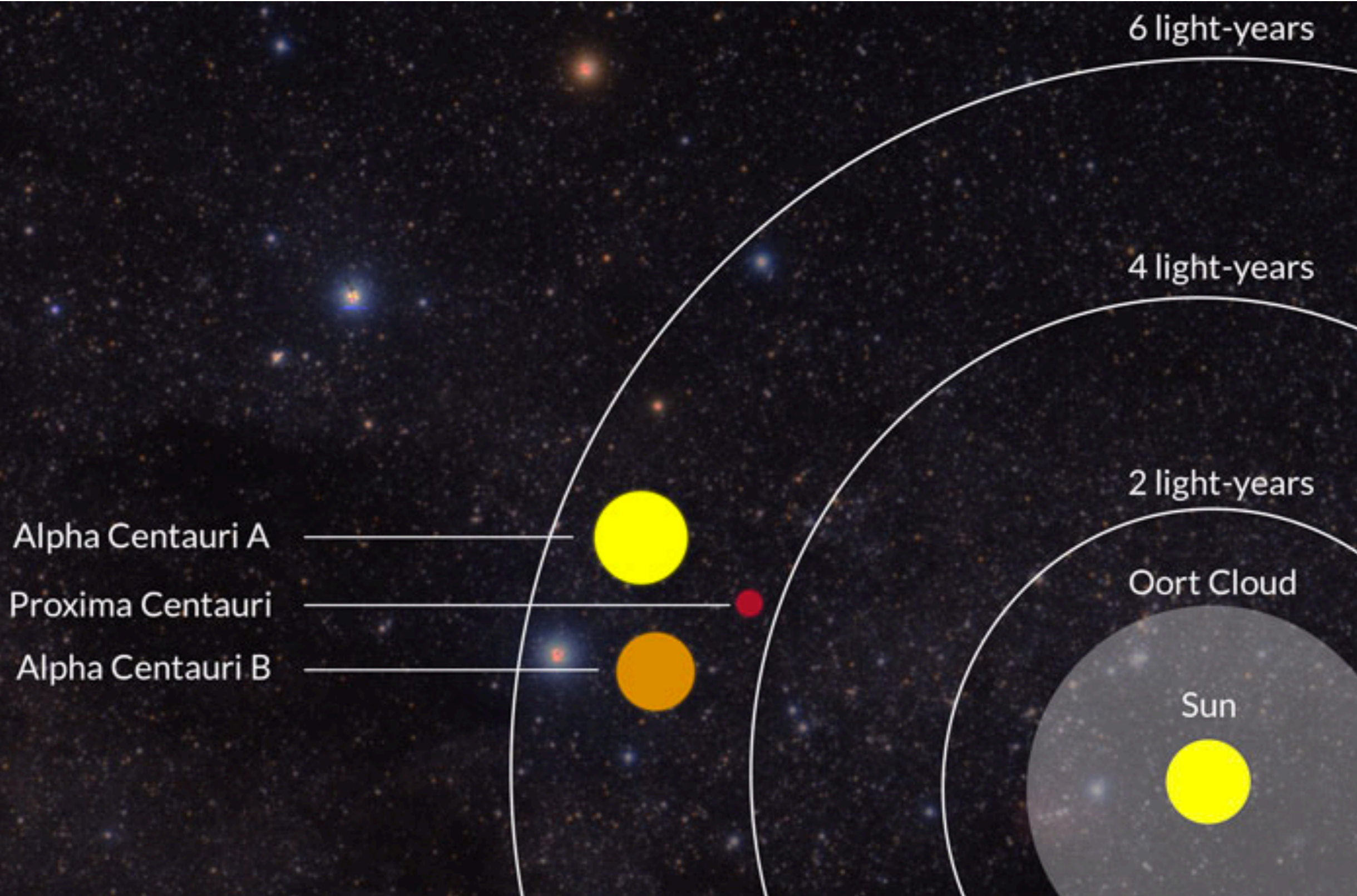
Evolution of stellar triples



Faculty (Amsterdam) - toonens@uva.nl - Vidi laureate

Tjarda Boekholt (Oxford), Nathan Leigh (Conception), Yan Gao (Birmingham),
Simon Portegies Zwart (Leiden), Christian Knigge (Southampton)

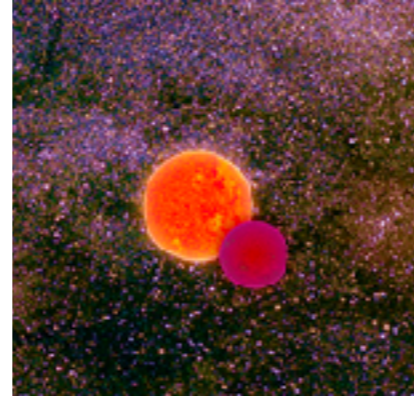
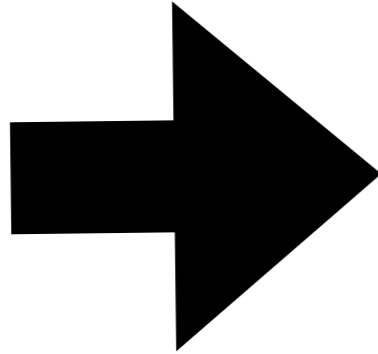
Our nearest neighbour...



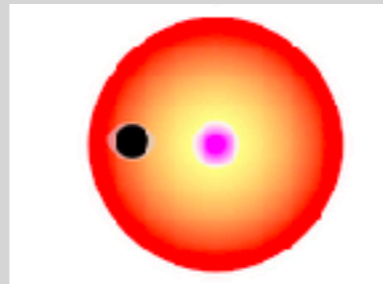
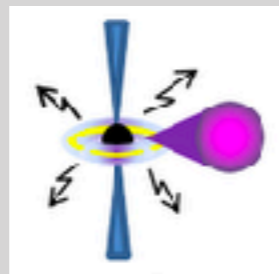
Single stars

Binaries

Triples



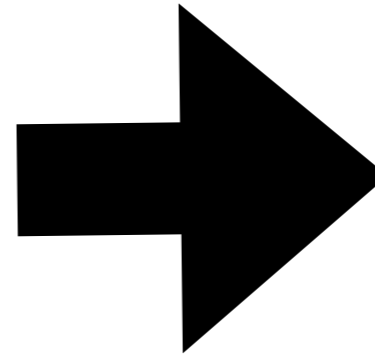
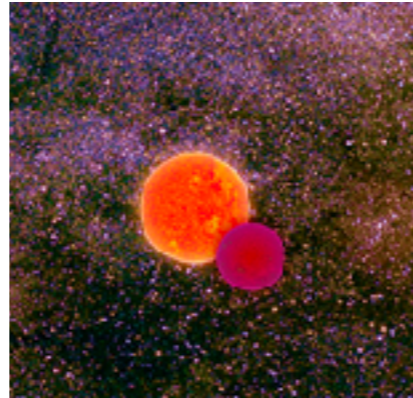
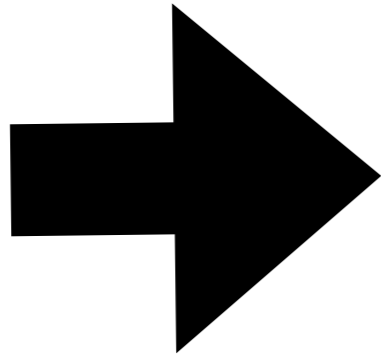
Stellar interactions, e.g.:



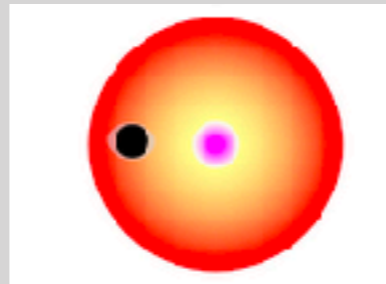
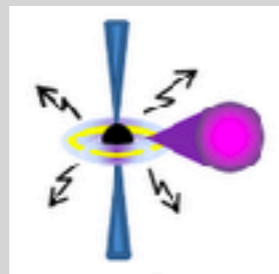
Single stars

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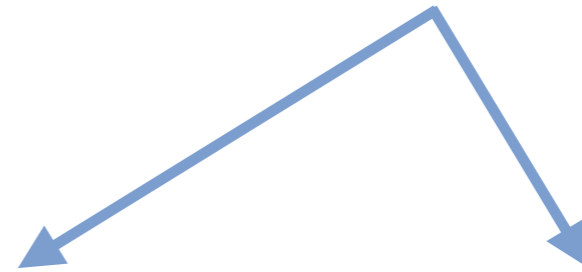
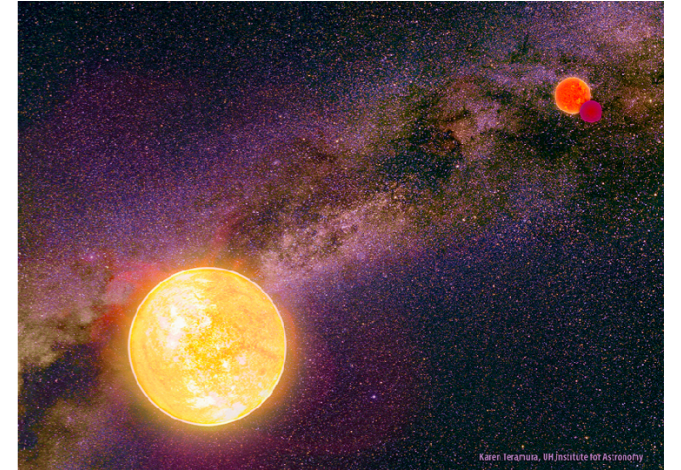
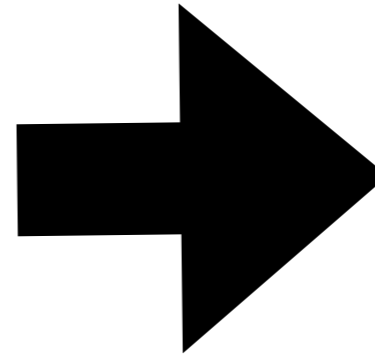
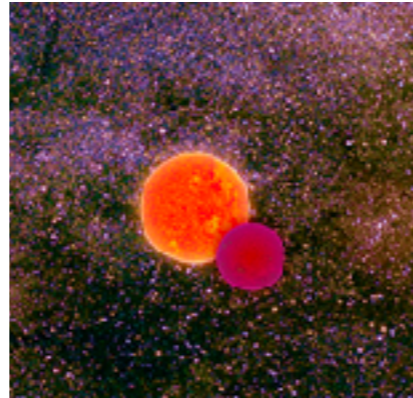
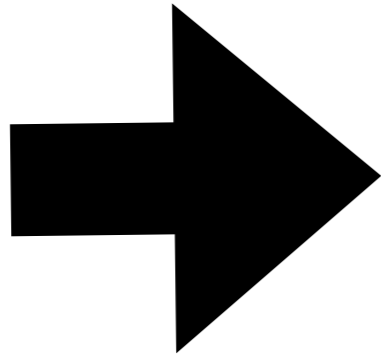
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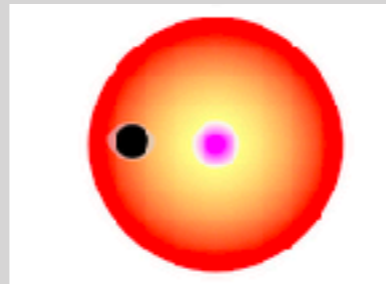
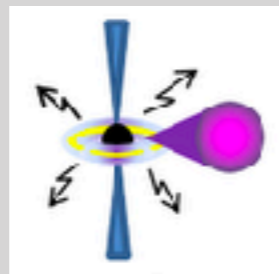
Single stars

Binaries

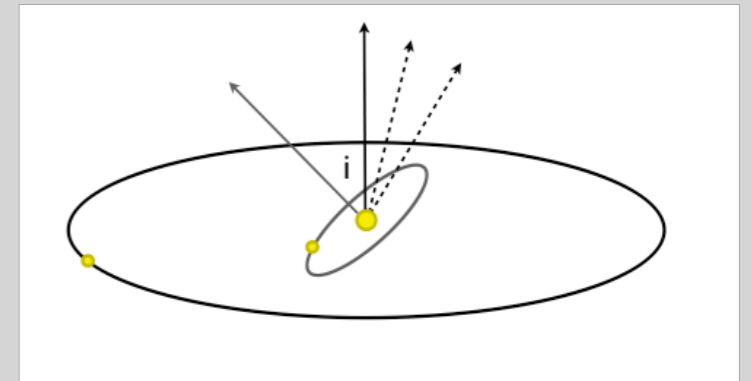
Triples



Stellar interactions, e.g.:



Orbital interactions:



3-body dynamics

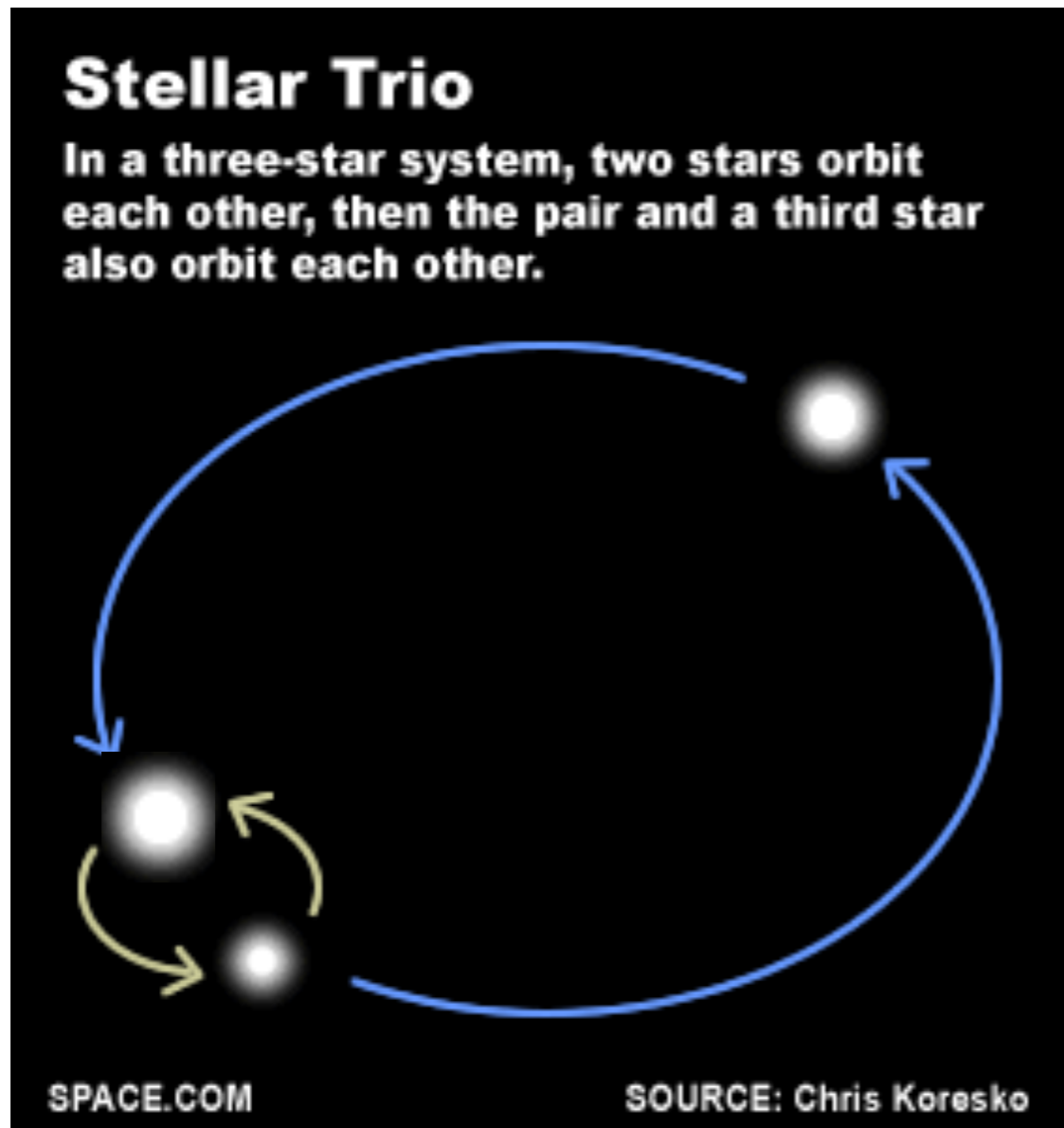
➔ The observational revolution calls for a higher accuracy in theoretical astronomy

Outline

1. Triple intro
 - ❖ Why care about stellar triples
 - ❖ How do triples evolve differently than binaries?
2. Typical evolution of triples & applications of triple evolution
 - ❖ Cataclysmic variables, barium stars, gravitational wave sources etc.

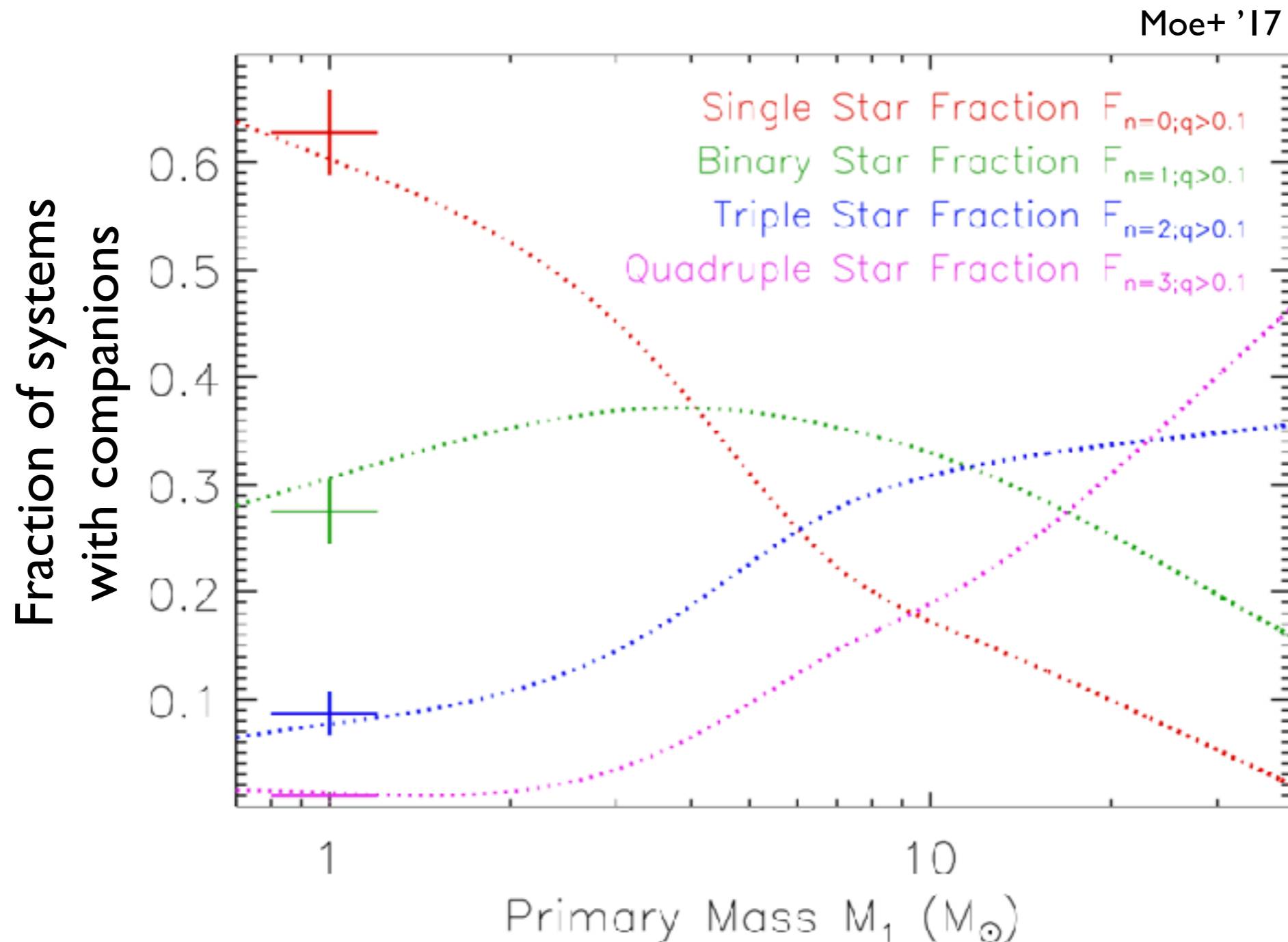


Stellar triples



- ❖ Isolated
- ❖ Stable $P_{\text{outer}} \gtrsim 5P_{\text{inner}}$
 - ❖ inner & outer orbit
- ❖ Abundant

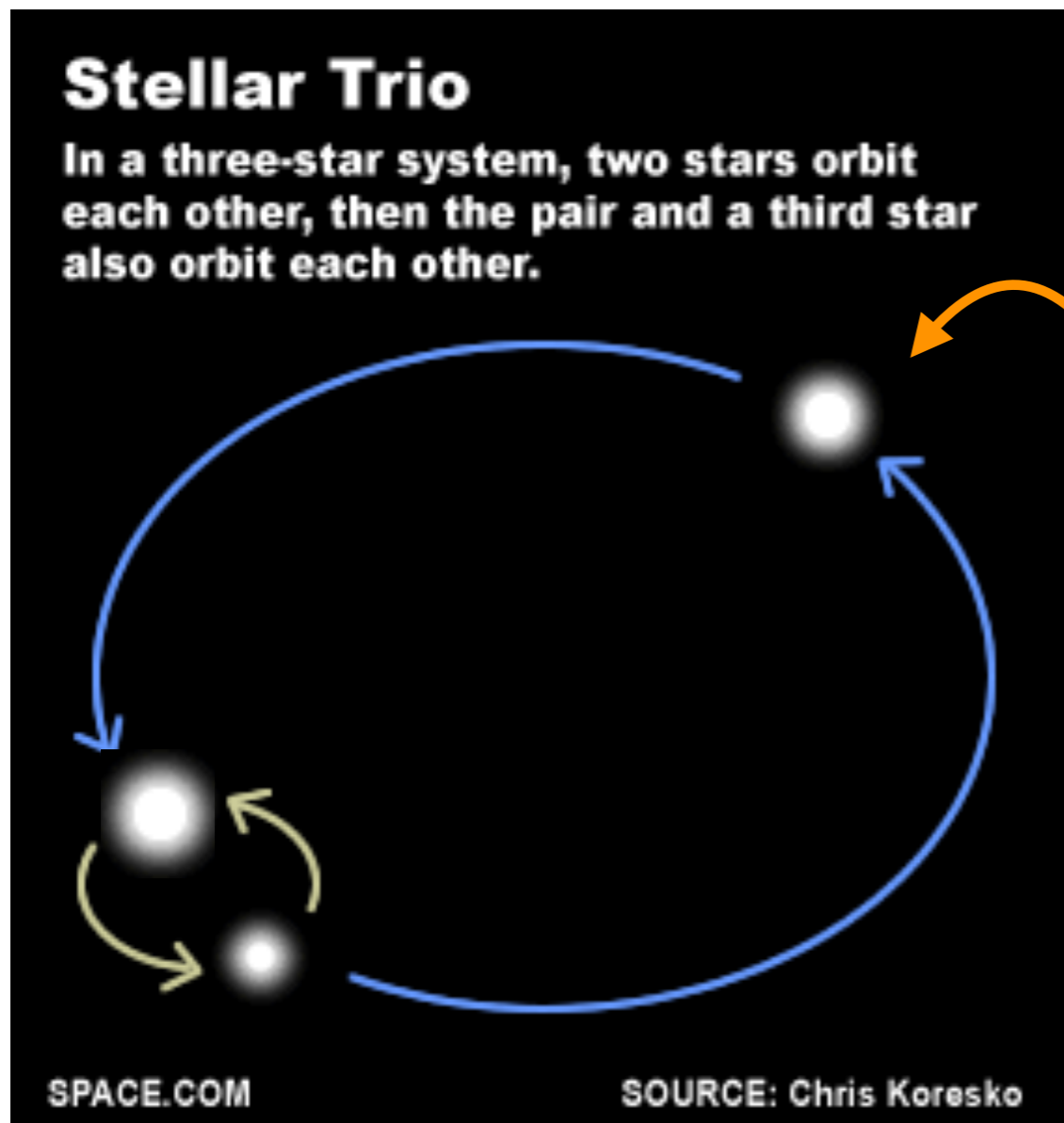
Abundance



Initial distribution - young systems

Raghavan+ '10, Tokovinin '08, '14, Evans '05, Duchene & Kraus '13, Sana+ '14, Moe+ '17

Stellar triples



- ❖ Triple evolution poorly understood, but recent progress
- ❖ Not only physical interactions play a role, but first level where orbital interactions play a role.
- ❖ Strong effect on inner binary. How? When?

Triple evolution

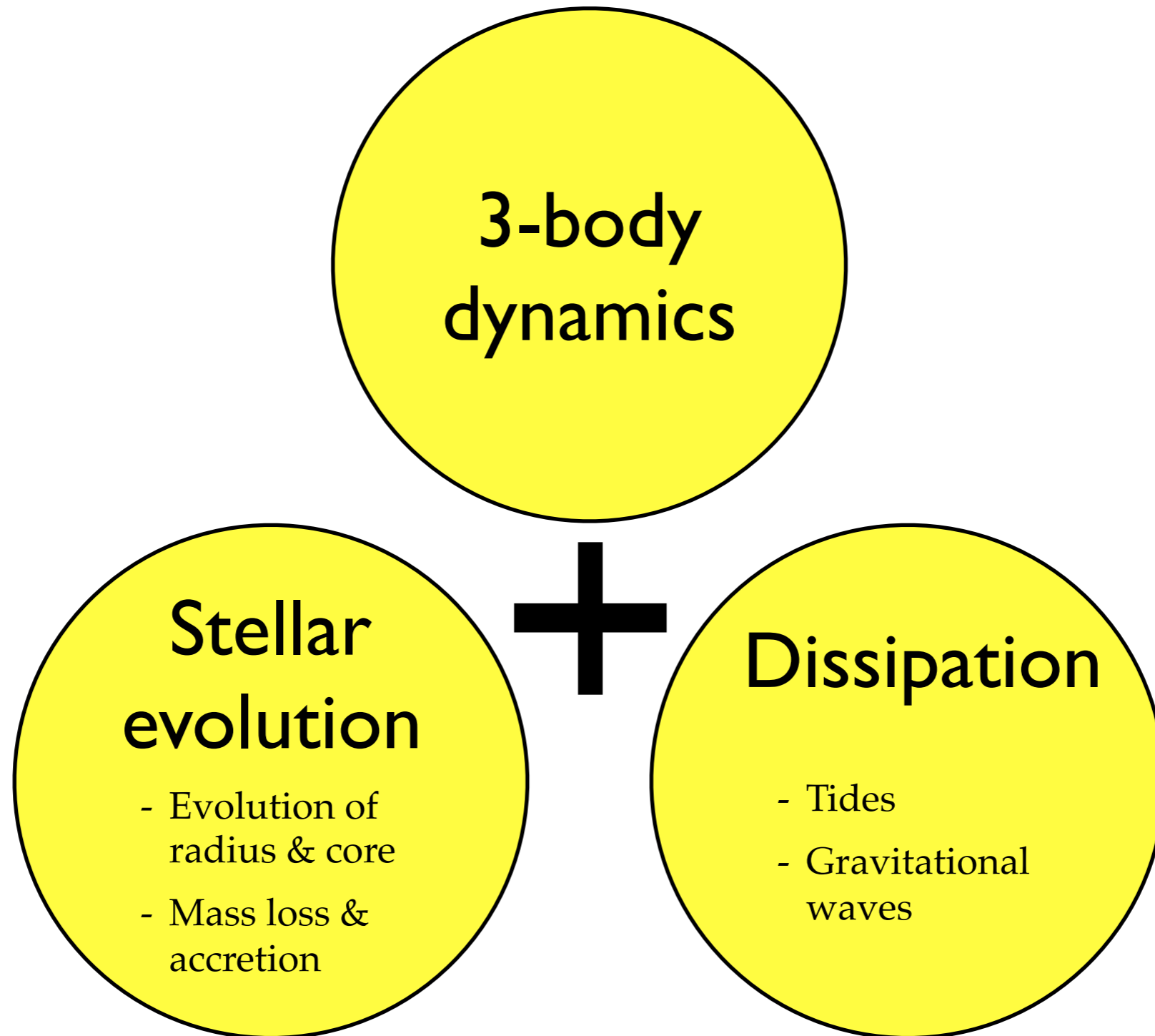
fragmented & incomplete

3-body problem
no analytical solution

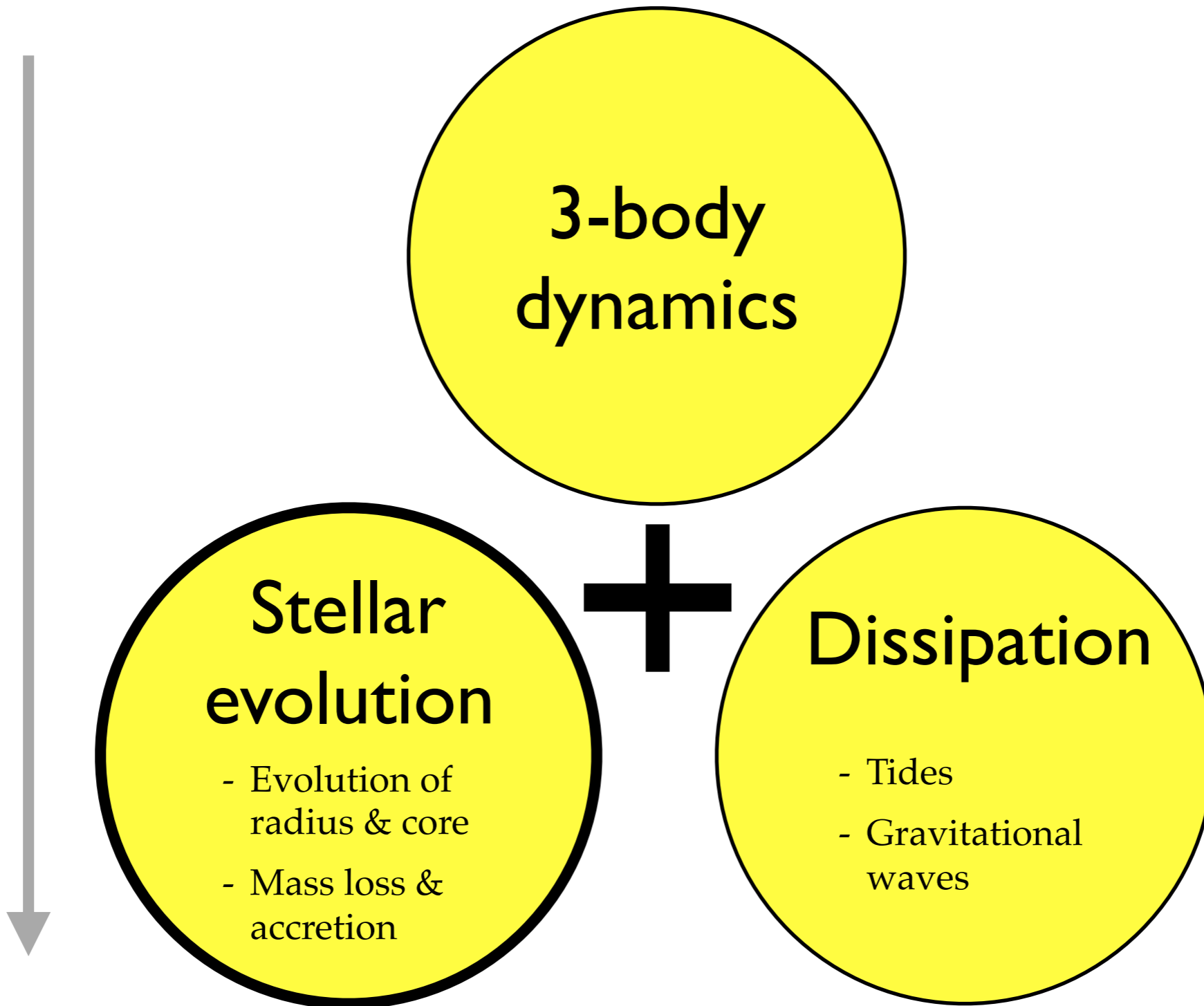
e.g. Valtonen &
Karttunen '06, Naoz+ 16

**3-body
dynamics**

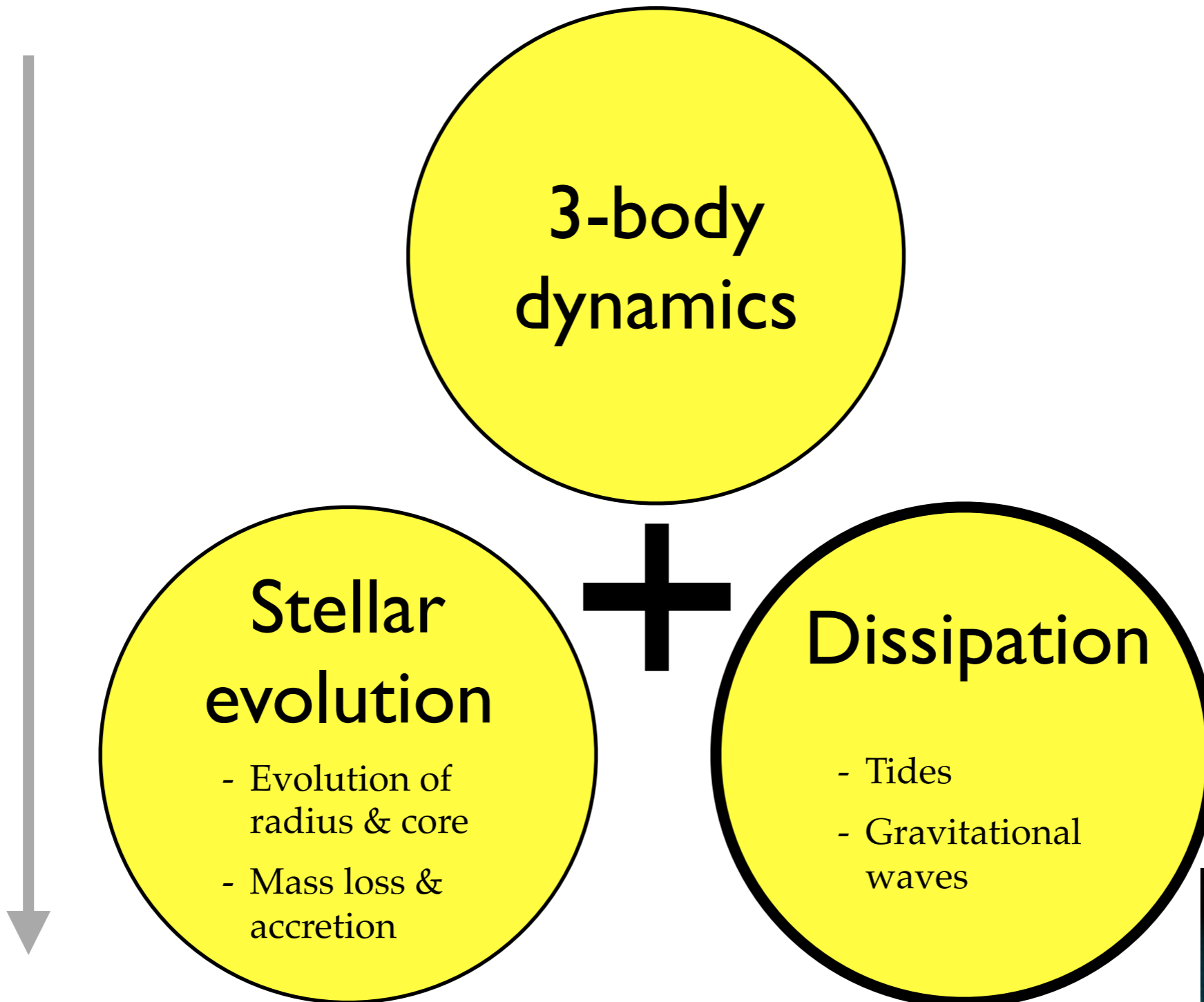
Triple evolution



Triple evolution



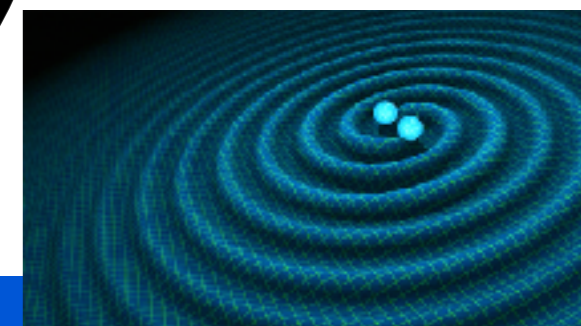
Triple evolution



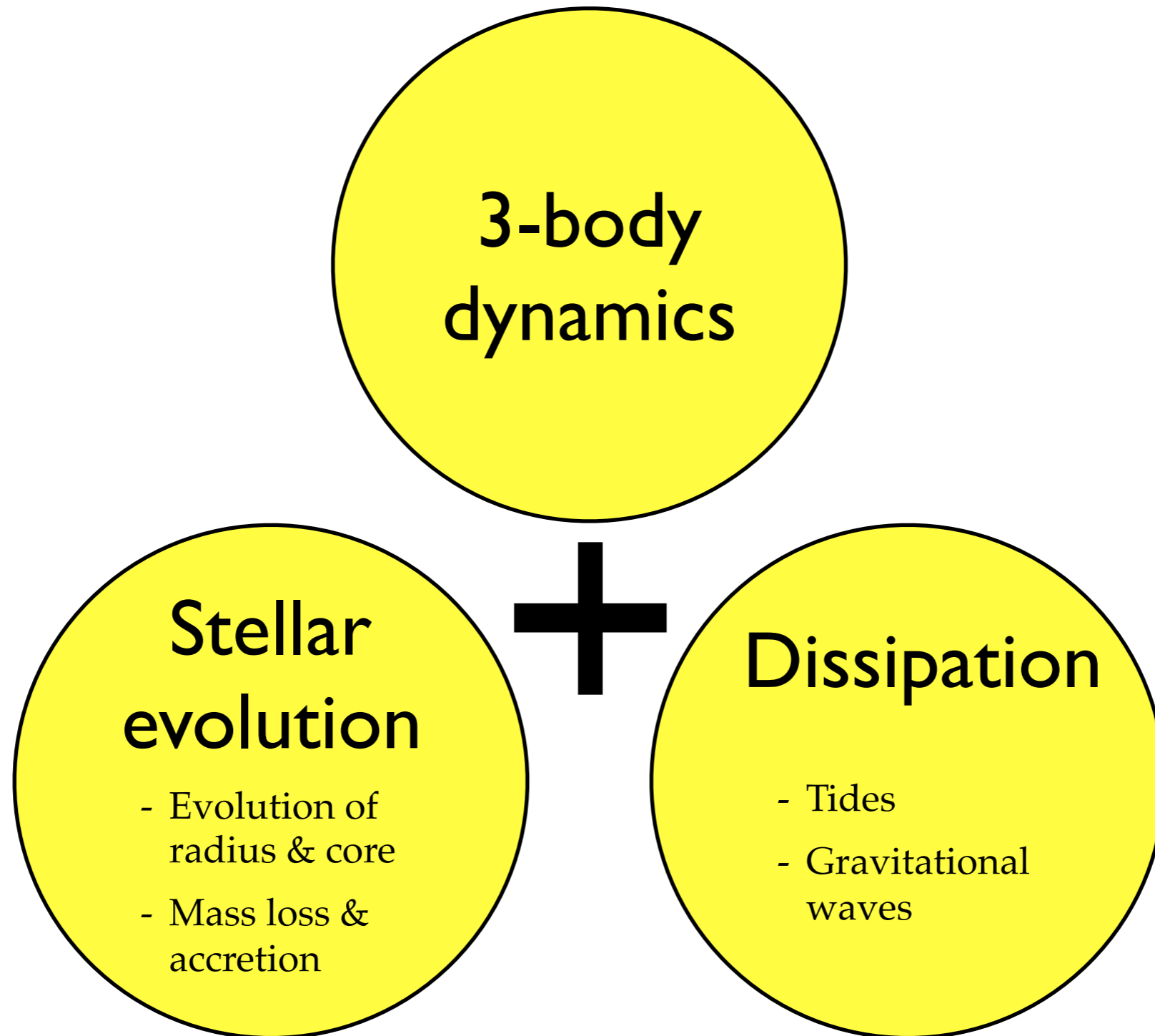
Tides effective when:
radius \sim orbit



Gravitational waves effective when:
orbit small



Triple evolution



Triple code TRES

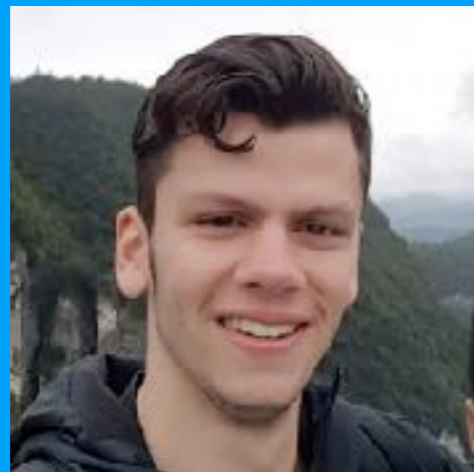
- ❖ Common evolution (Toonen+ '20)
- ❖ Supernova type Ia (Toonen+ '18)
- ❖ BH-BH mergers (Antonini, Toonen+ '17)
- ❖ Sequential mergers (Vigna-Gomez+ '20)
- ❖ Circumbinary planets (Columba+ '23)
- ❖ Unstable triples (Toonen+ 2022)
- ❖ Formation of cataclysmic variables (Knigge+ 2022)
- ❖ Formation of Barium stars (Gao+ '23)
- ❖ Massive stars (Kummer+ subm)

TRES core team

Tjarda Boekholt

Silvia Toonen, PI

Simon Portegies Zwart

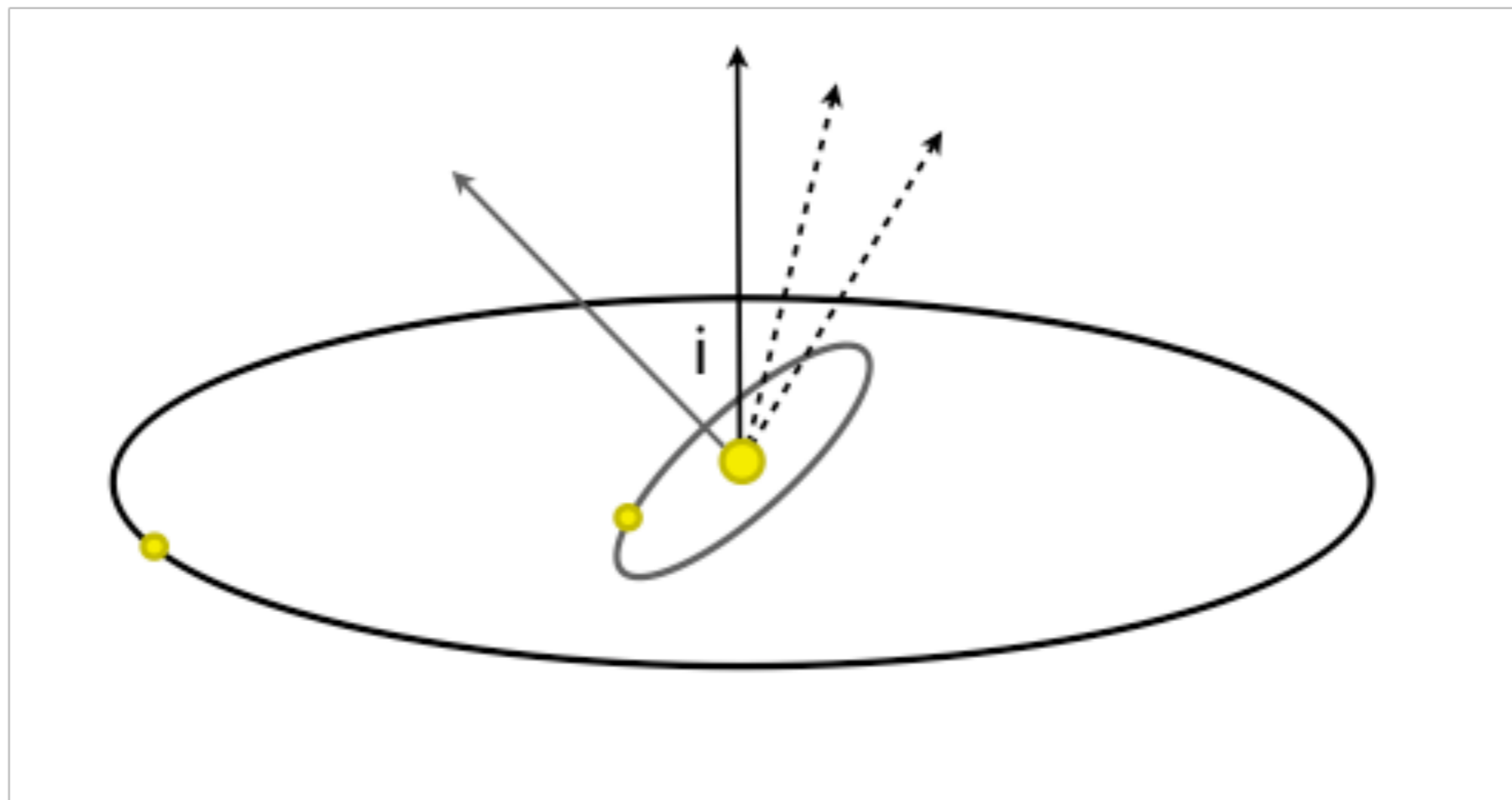
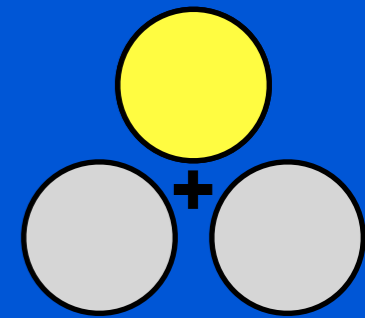


Floris Kummer

Andris Dorozsmai

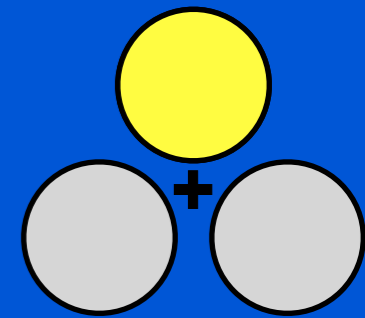
Caspar Bruenech

3-Body dynamics



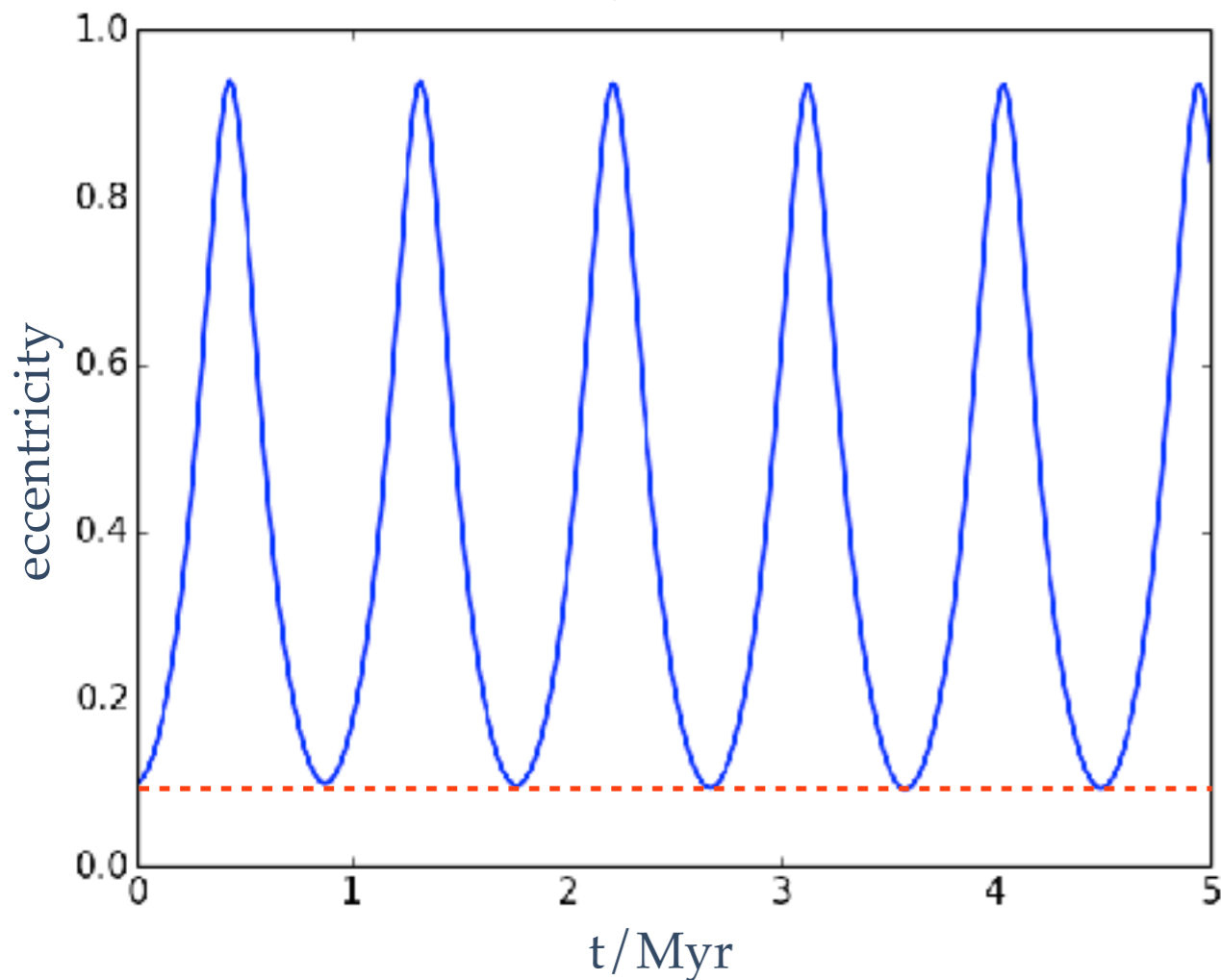
- Kozai-Lidov cycles (Lidov '62, Kozai '62) $P_{\text{KL}} \sim \frac{P_{\text{outer}}^2}{P_{\text{inner}}} \frac{m_1 + m_2 + m_3}{m_3} (1 - e_{\text{outer}}^2)^{3/2}$
- Higher-order effects: more extreme eccentricities, orbital flips (see review of Naoz+ 16)

Kozai-Lidov cycles

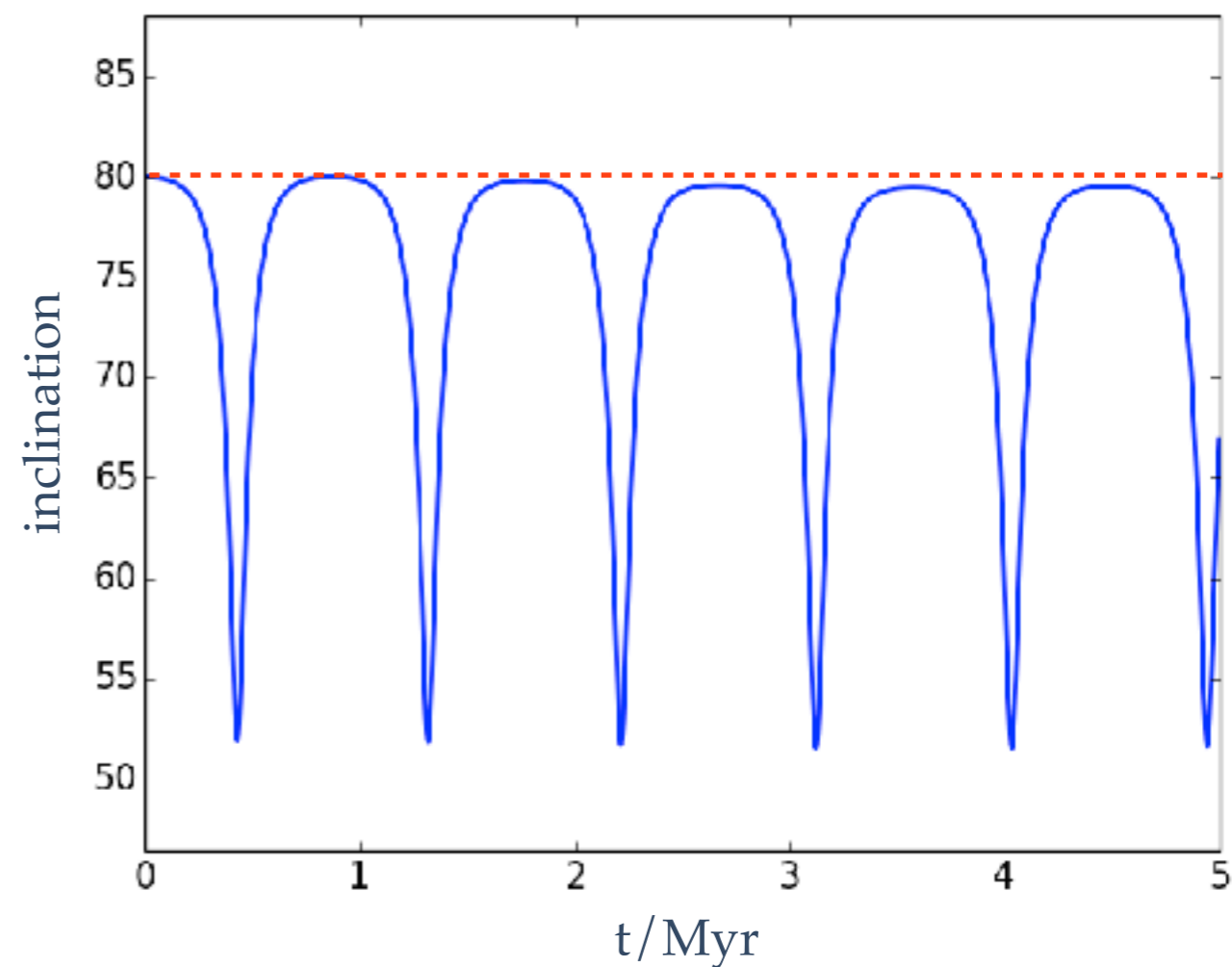


example: $M_1=1.3$, $M_2=0.5$, $M_3=0.5M_{\text{Sun}}$, $a_1=200$, $a_2=20000R_{\text{Sun}}$, $e_1=0.1$, $e_2=0.5$, $i=80$, $g_1=0.1$, $g_2=0.5$

Eccentricity inner orbit



Mutual inclination

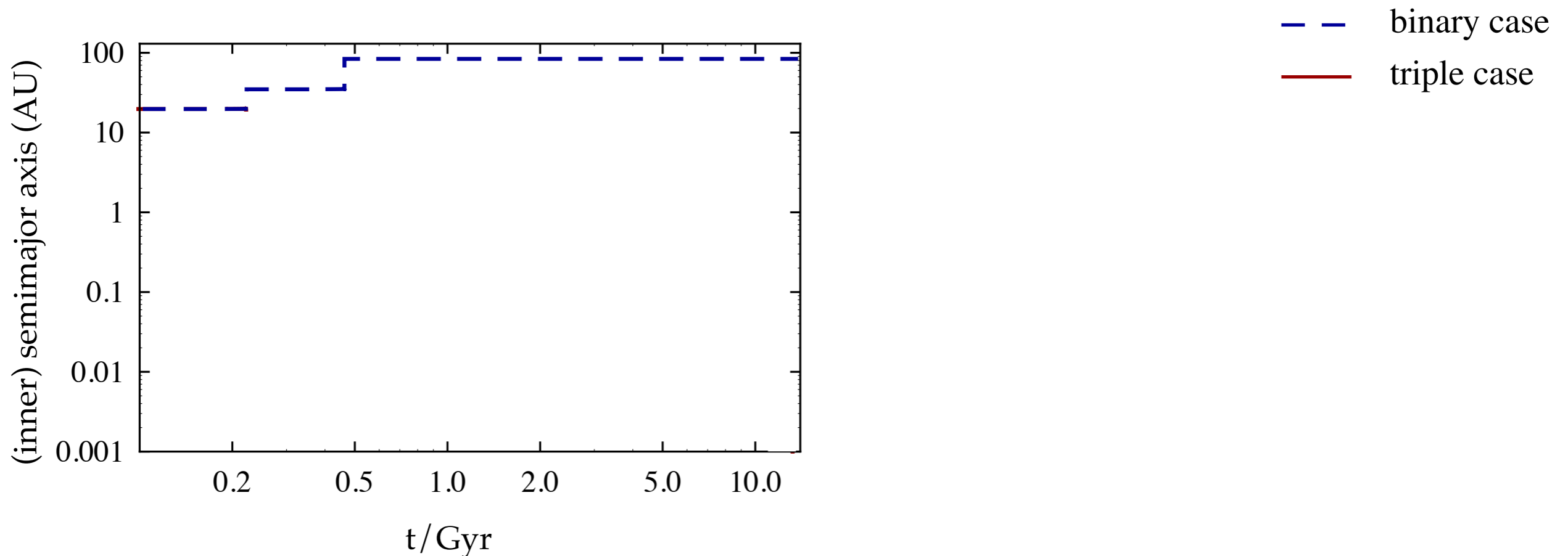


--- Binary case
— Triple case

$$P_{\text{KL}} \sim \frac{P_{\text{outer}}^2}{P_{\text{inner}}} \frac{m_1 + m_2 + m_3}{m_3} (1 - e_{\text{outer}}^2)^{3/2}$$

Long-term effect

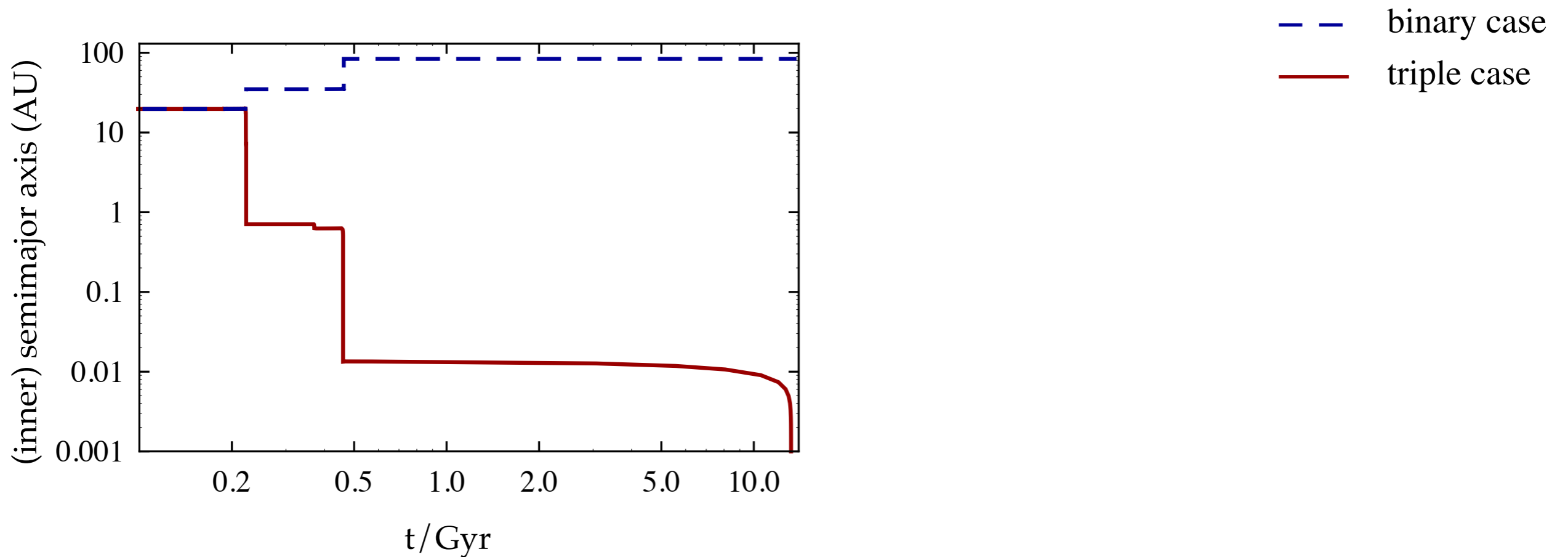
example: $M_1=3.95$, $M_2=3.03$, $M_3=2.73M_{\text{Sun}}$, $a_1=19.7$, $a_2=636\text{AU}$, $e_1=0.23$, $e_2=0.82$, $i=116$



courtesy of Adrian Hamers

Long-term effect

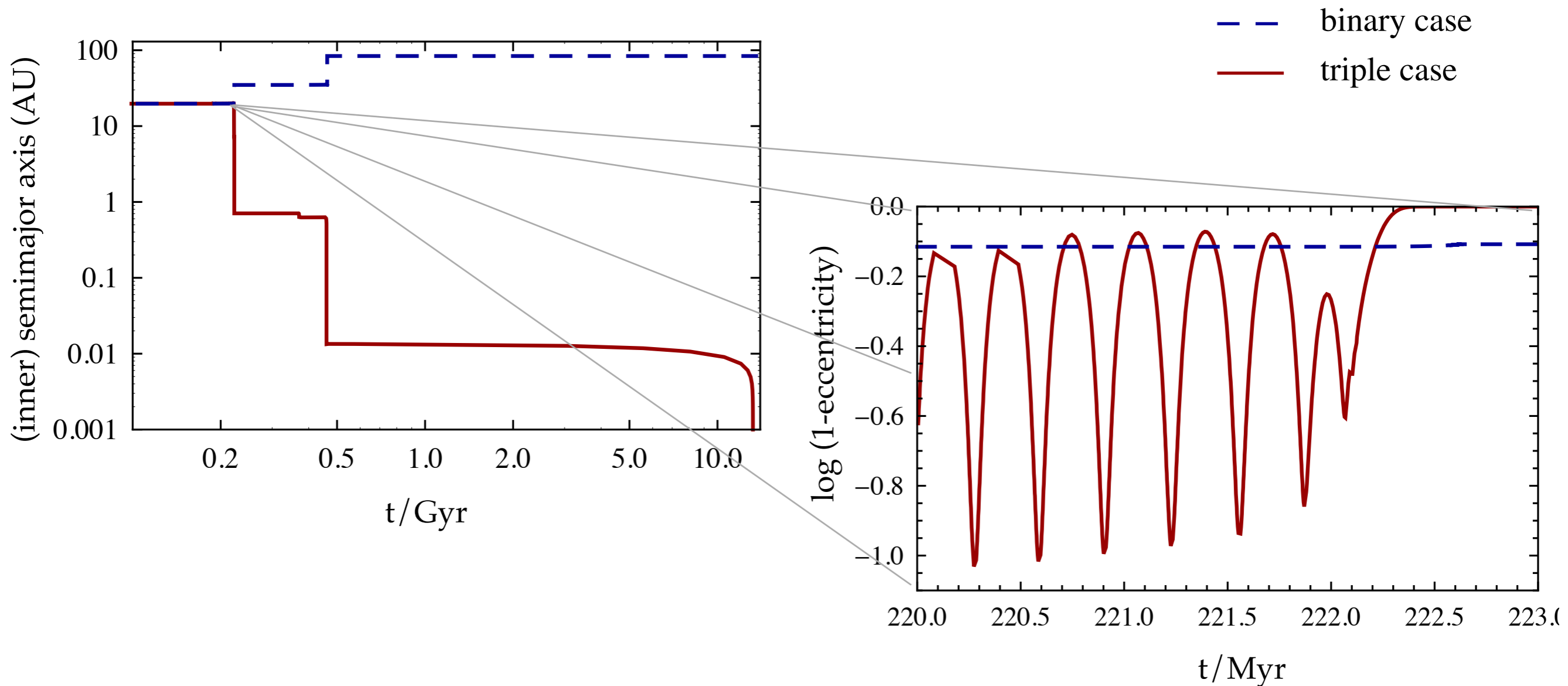
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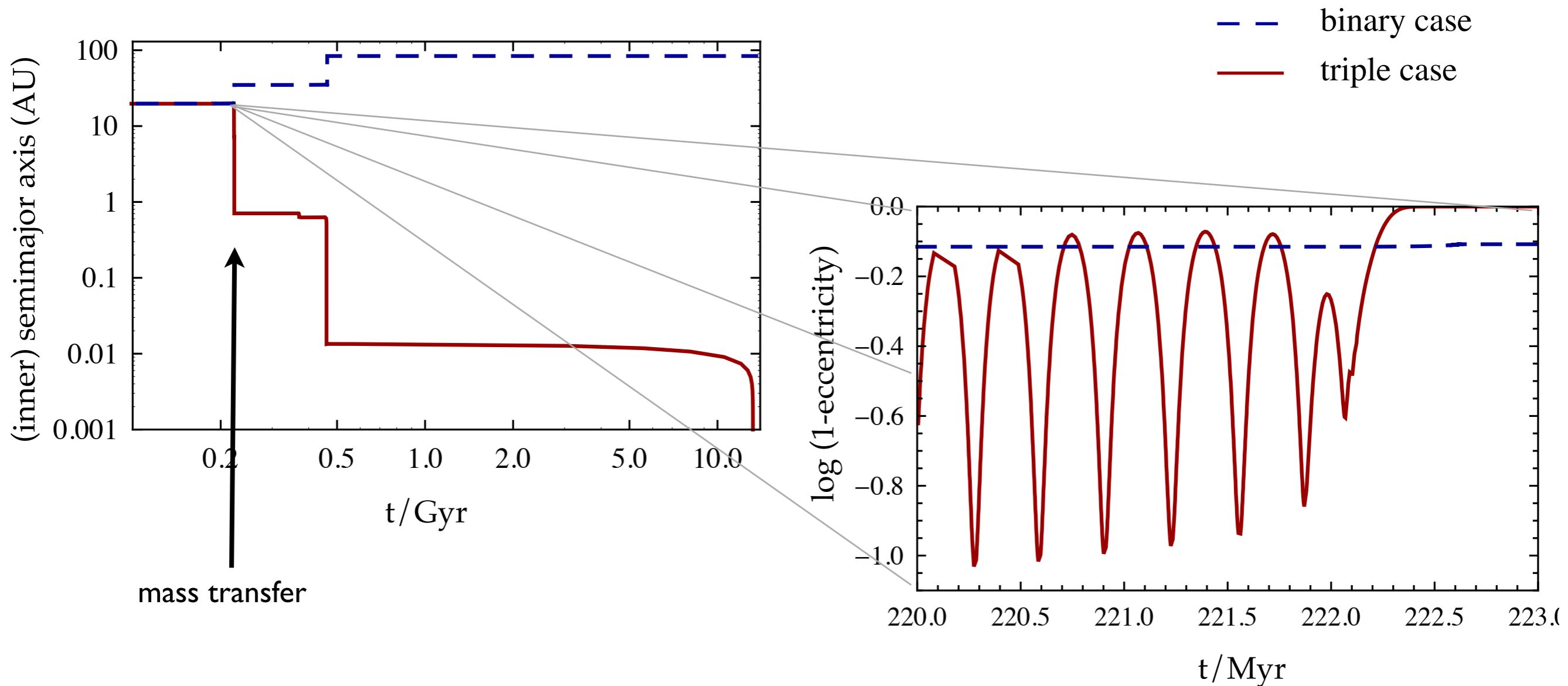
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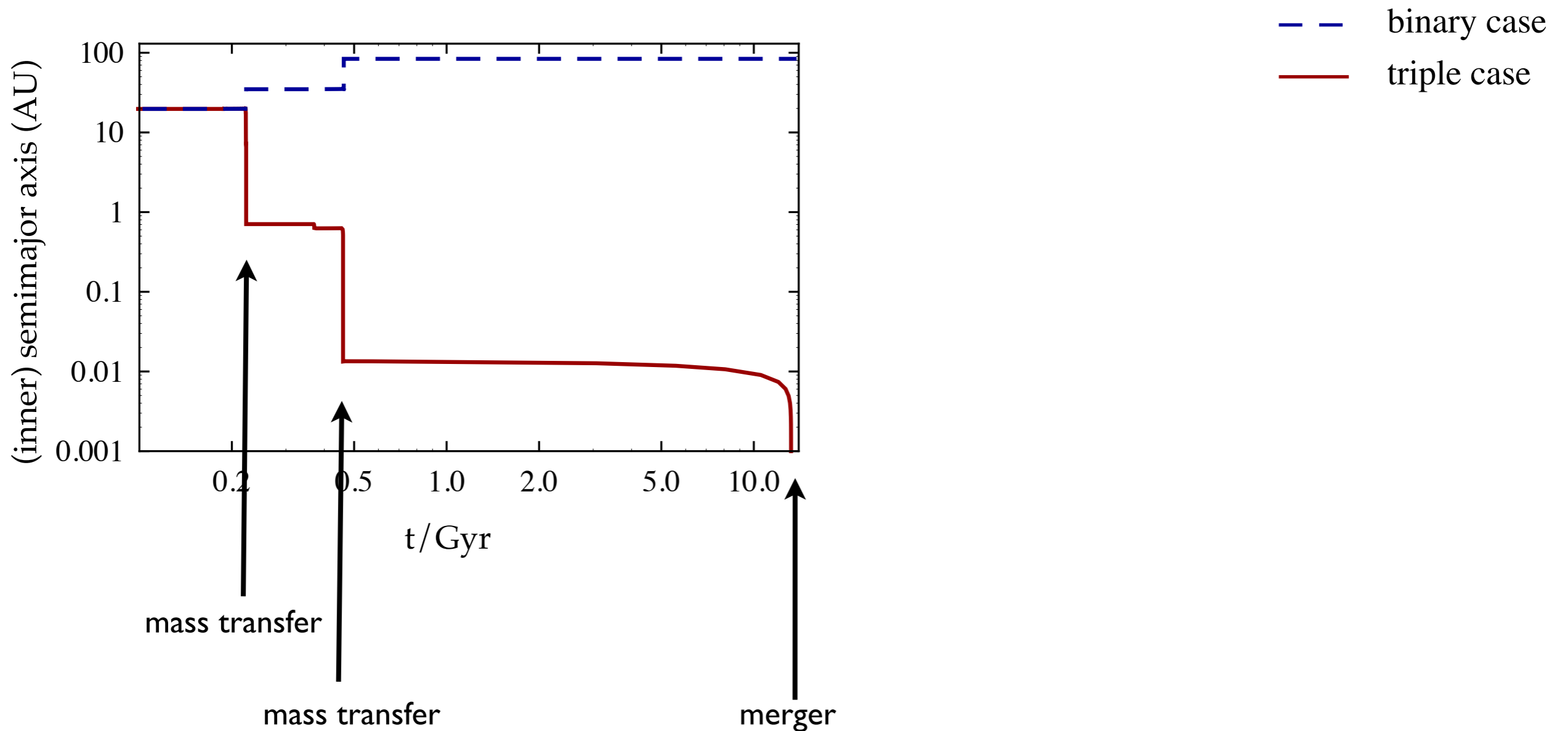
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- ❖ Cataclysmic variables, barium stars, gravitational wave sources etc.



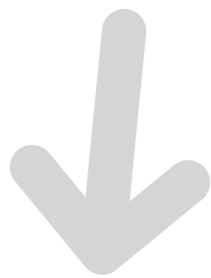
Typical evolution of triples

- ❖ low & intermediate mass primaries ($1-7.5M_{\odot}$)

Typical evolution of triples

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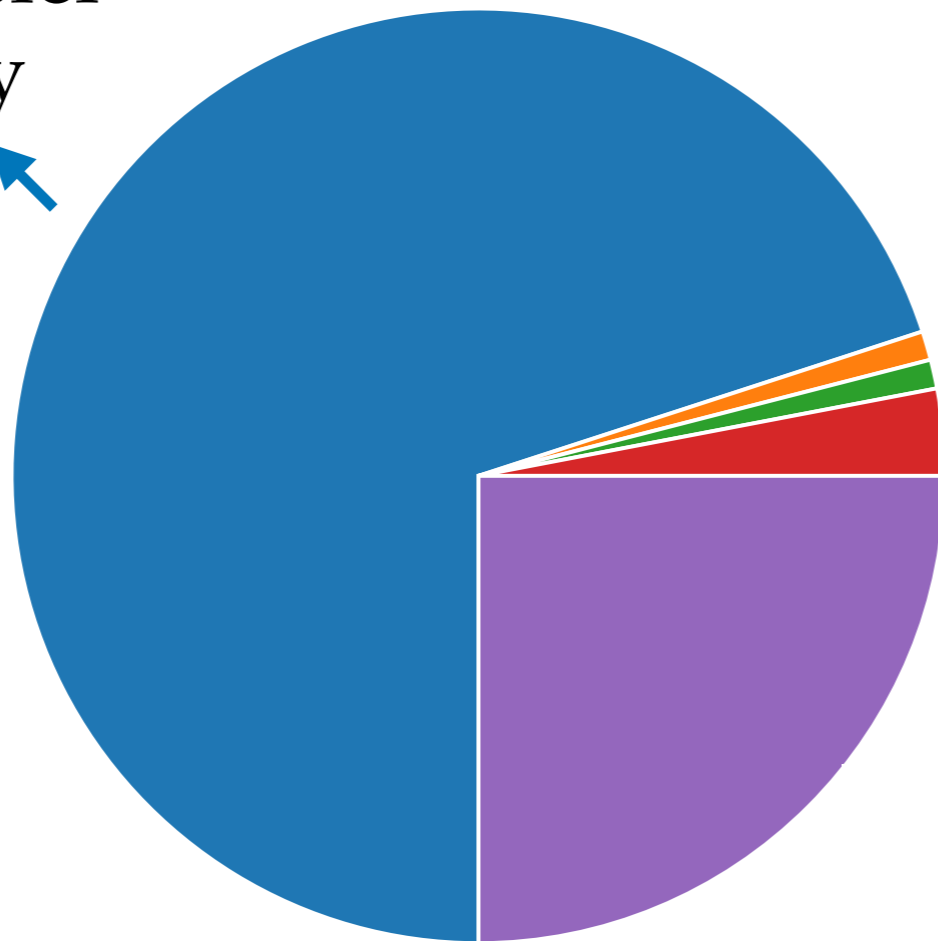
Mass transfer
by primary
 $\sim 64-75\%$



In binaries:

only $\sim 28-39\%$

- $N(P) \propto 1/P$
- $N(P) \propto \text{log-normal}(P)$



Take-home message

For every 3 binaries formed,
at least one triple is born

(Tokovinin+ '14, Moe+ '17)

Triples interact more
often than binaries!

(Toonen+ '20)

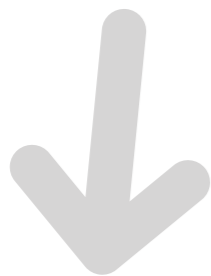


Triples on even footing with binaries

Typical evolution of triples

- low & intermediate mass primaries ($1-7.5M_{\odot}$)

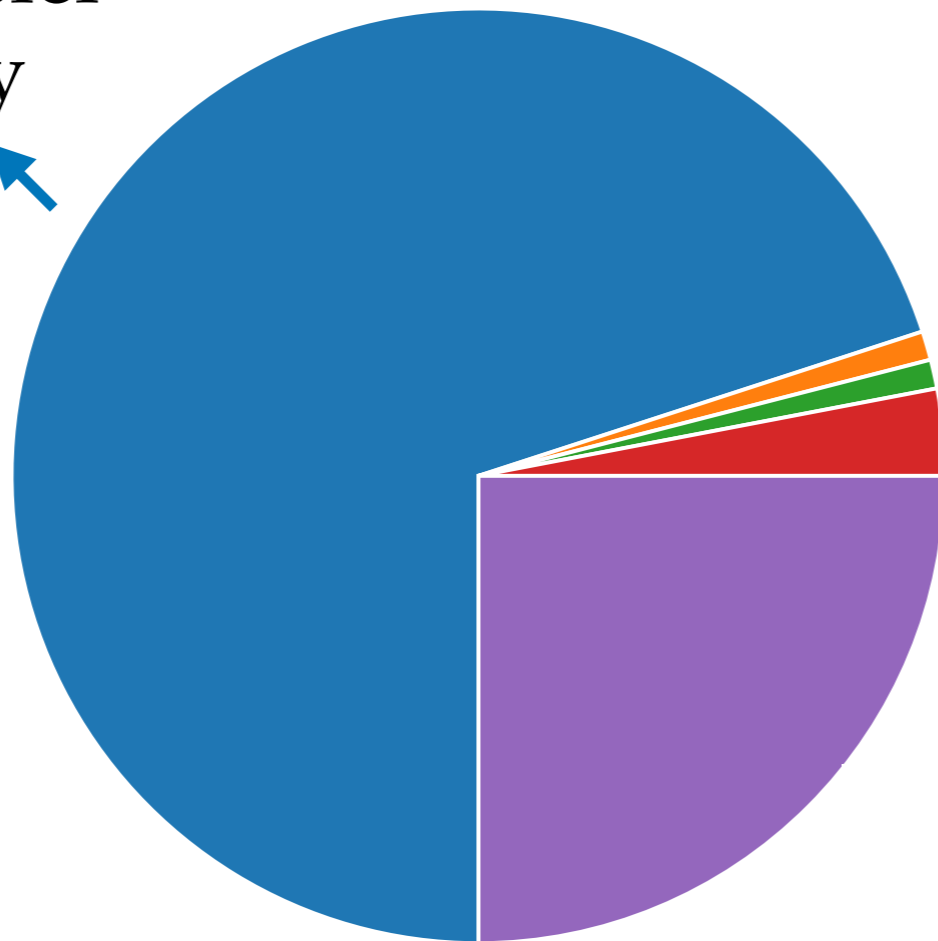
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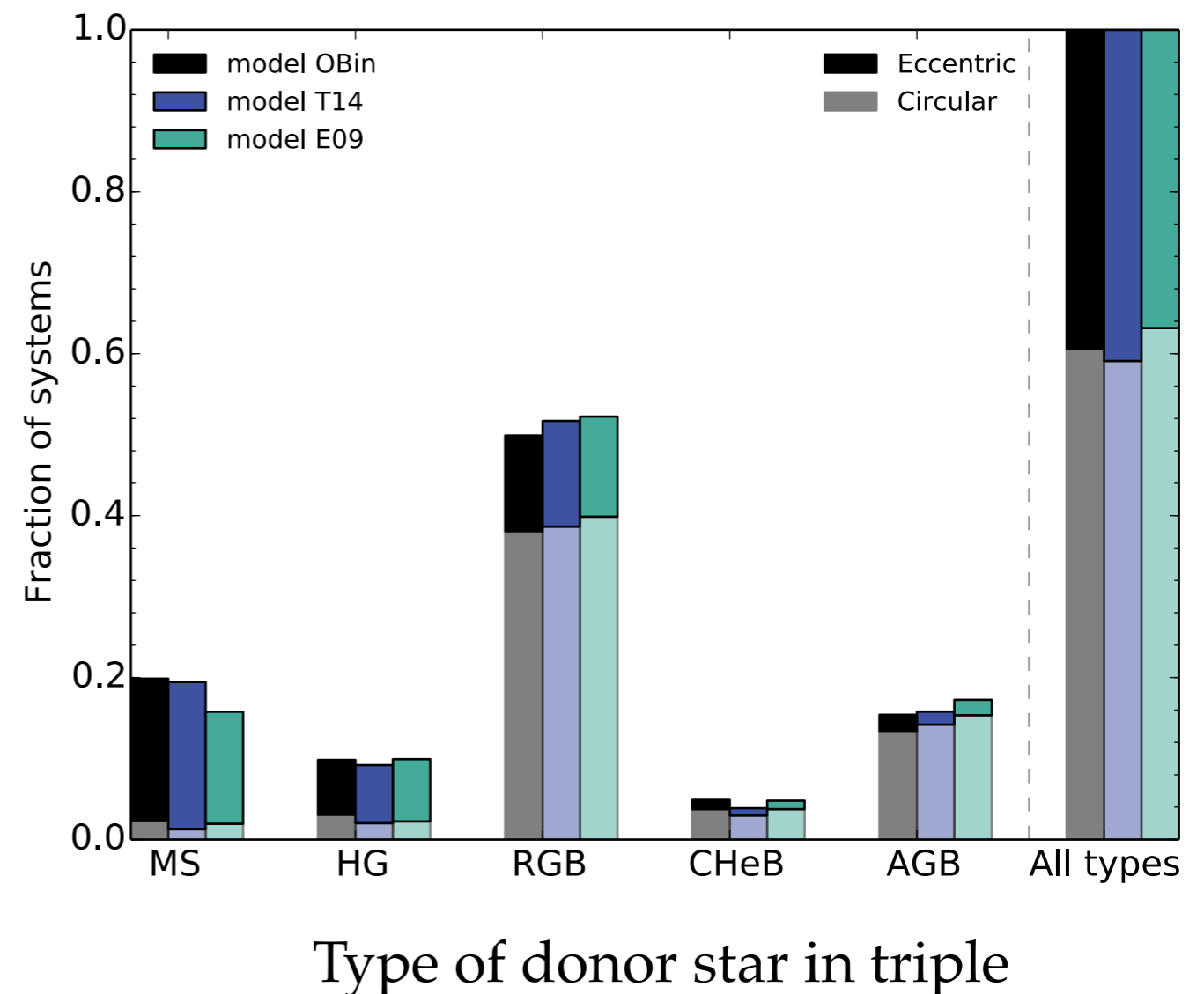
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- $N(P) \propto 1/P$
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Mass transfer

- ❖ Mass transfer common in triples
- ❖ Other differences with binaries?
 - ❖ Mass transfer occurs earlier
 - ❖ Orbit still eccentric upon onset of mass transfer



Mass transfer

- * Mass transfer common in triples
- * Other differences with binaries?
 - * Mass transfer occurs earlier
 - * Orbit still eccentric upon onset of mass transfer

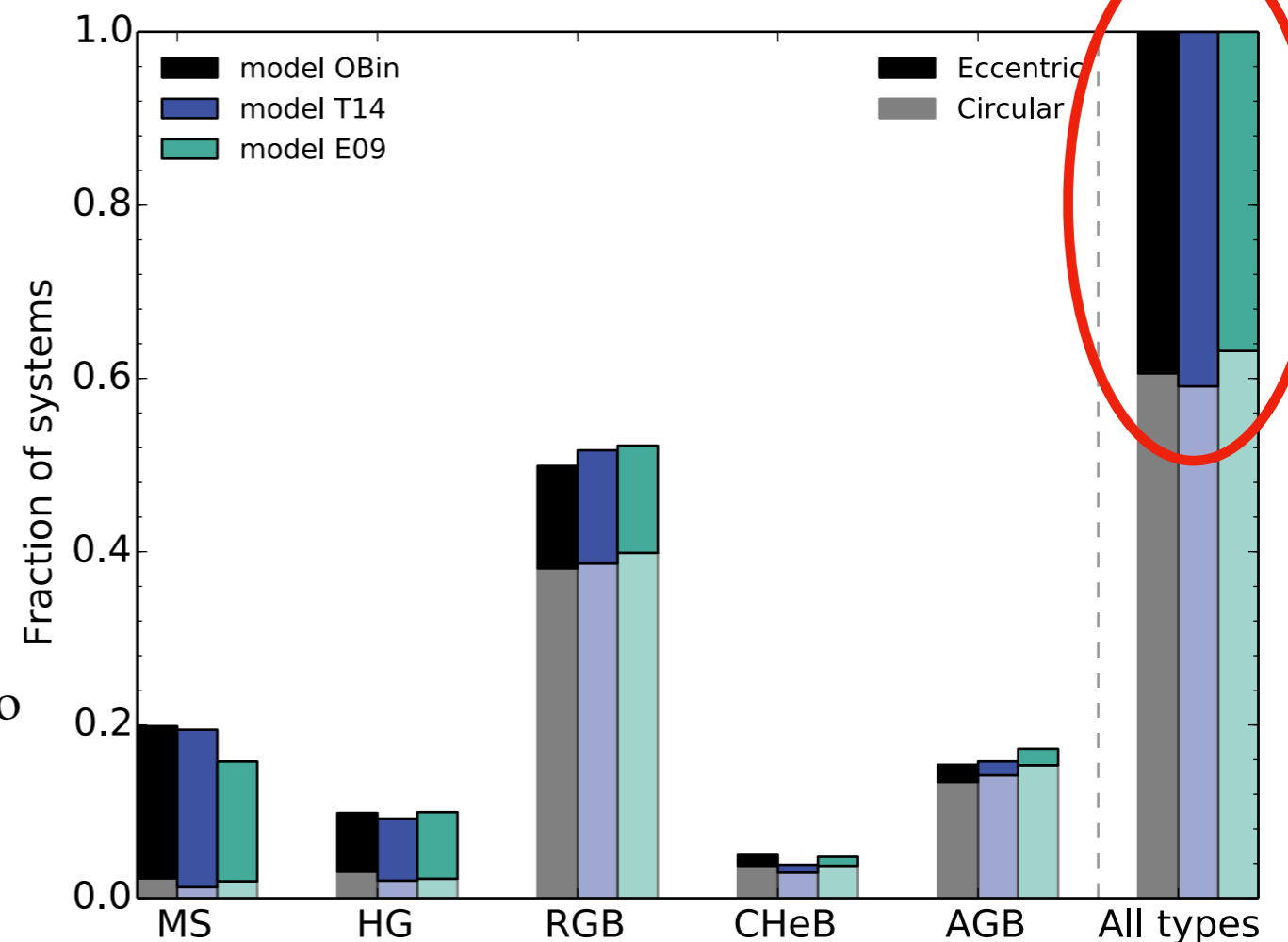
→ Observed sources

(e.g. Petrova & Orlov 1999,
Nicholls & Wood 2012)

→ Tides crucially important (see also Preece+ 22)

→ New framework needed for modelling eccentric mass transfer (Sepinsky+ '07, '09, '11, Dosopoulou+ '16, Hamers & Dosopoulou '19)

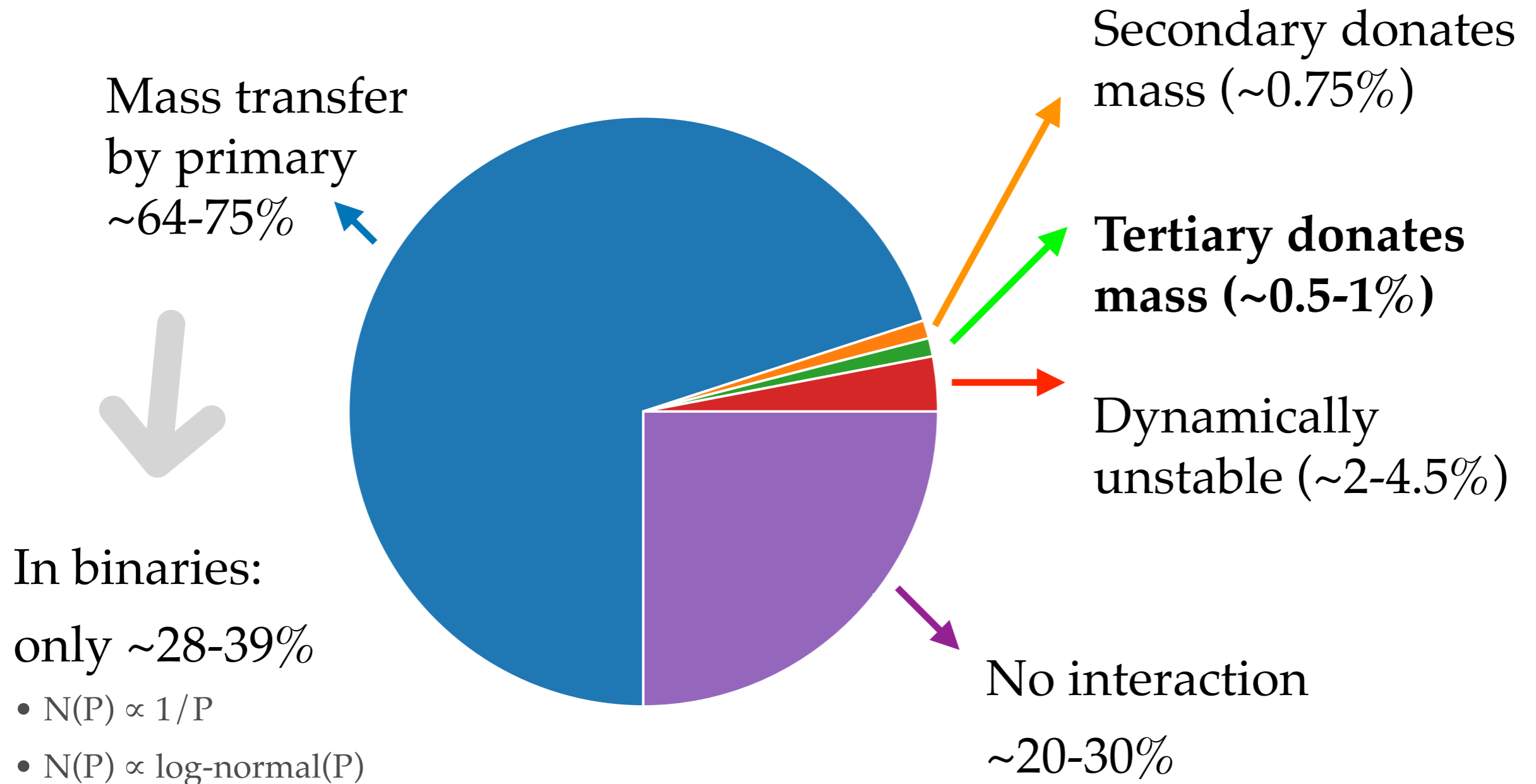
~40% still eccentric



Type of donor star in triple

Typical evolution of triples

- low & intermediate mass primaries ($1-7.5M_{\odot}$)



Evolution of triples

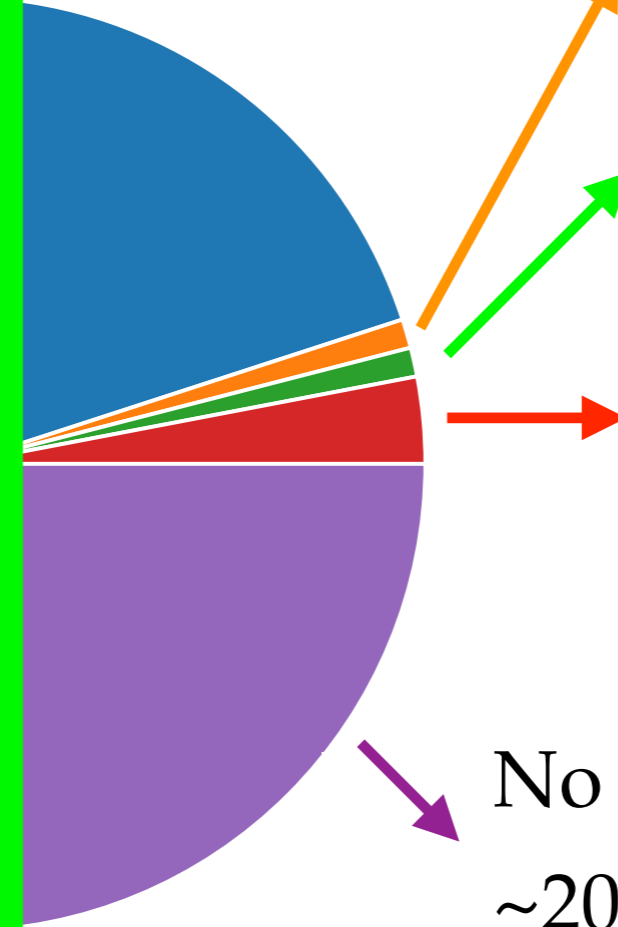
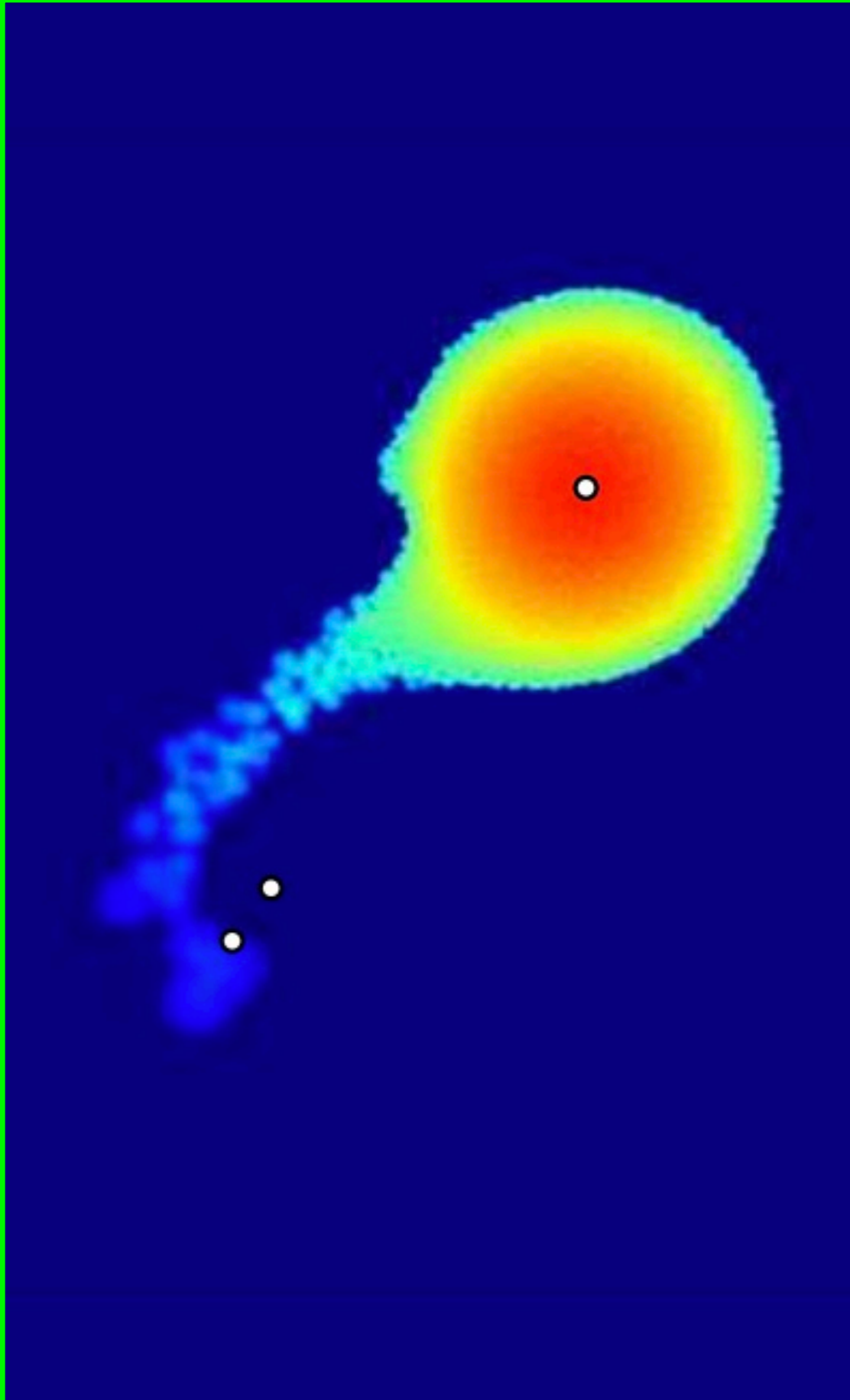
Primaries (1-7.5M_o)

Secondary donates mass (~0.75%)

Tertiary donates mass (~0.5-1%)

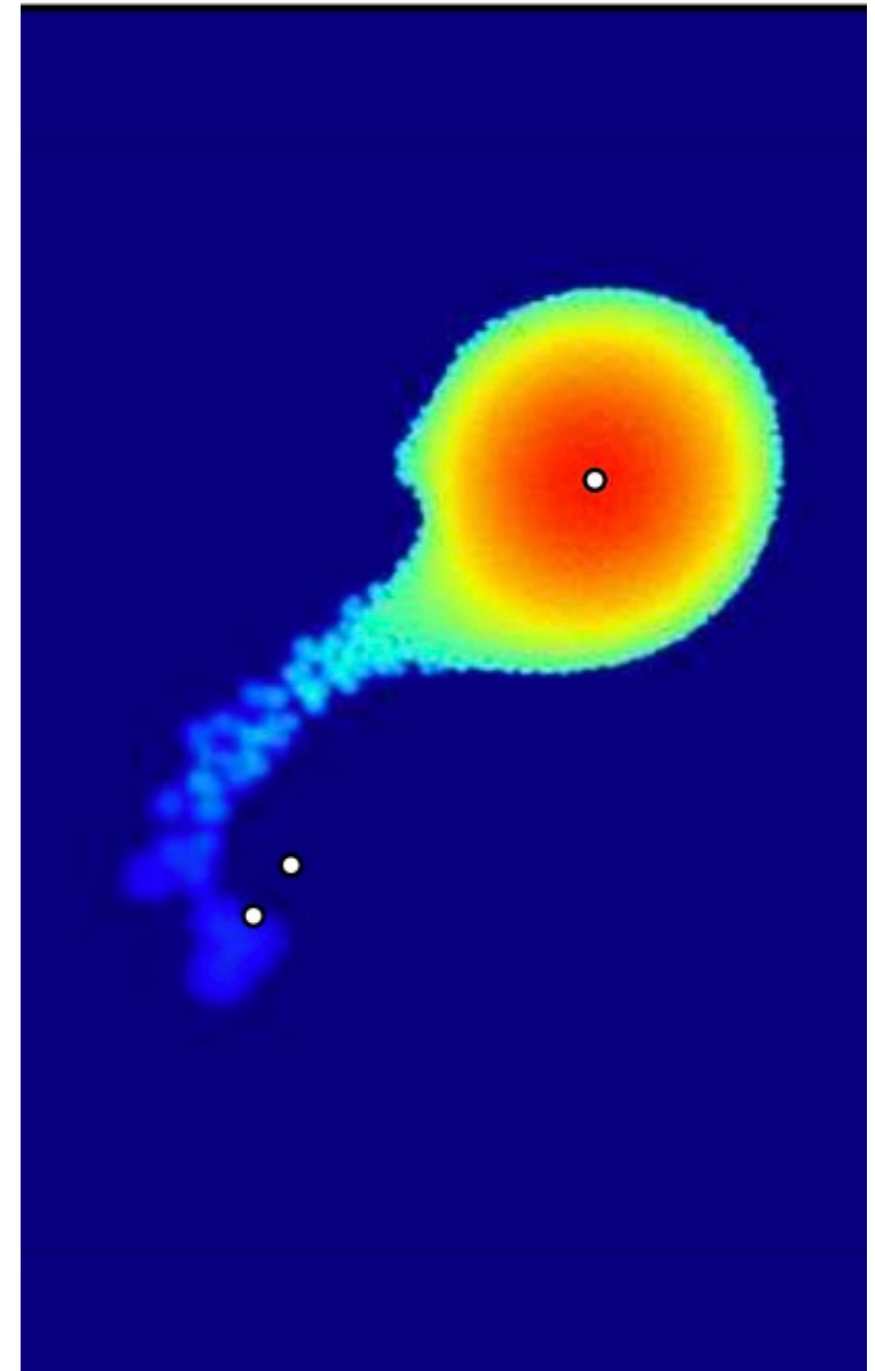
Dynamically unstable (~2-4.5%)

No interaction
~20-30%



Tertiary donates mass

- ❖ Frequency ($\sim 0.5-1\%$) consistent with observations of Tokovinin catalogue (De Vries+ '14)
- ❖ Creates twin blue stragglers through circum-binary disks (Portegies Zwart & Leigh '19)
- ❖ For other systems: based on binary modelling (Leigh+ w/Toonen '20):
 - $\sim 1\%$ of MS-MS
 - $\sim 1-5\%$ of WD-MS
 - $\sim 5-10\%$ of WD-WD



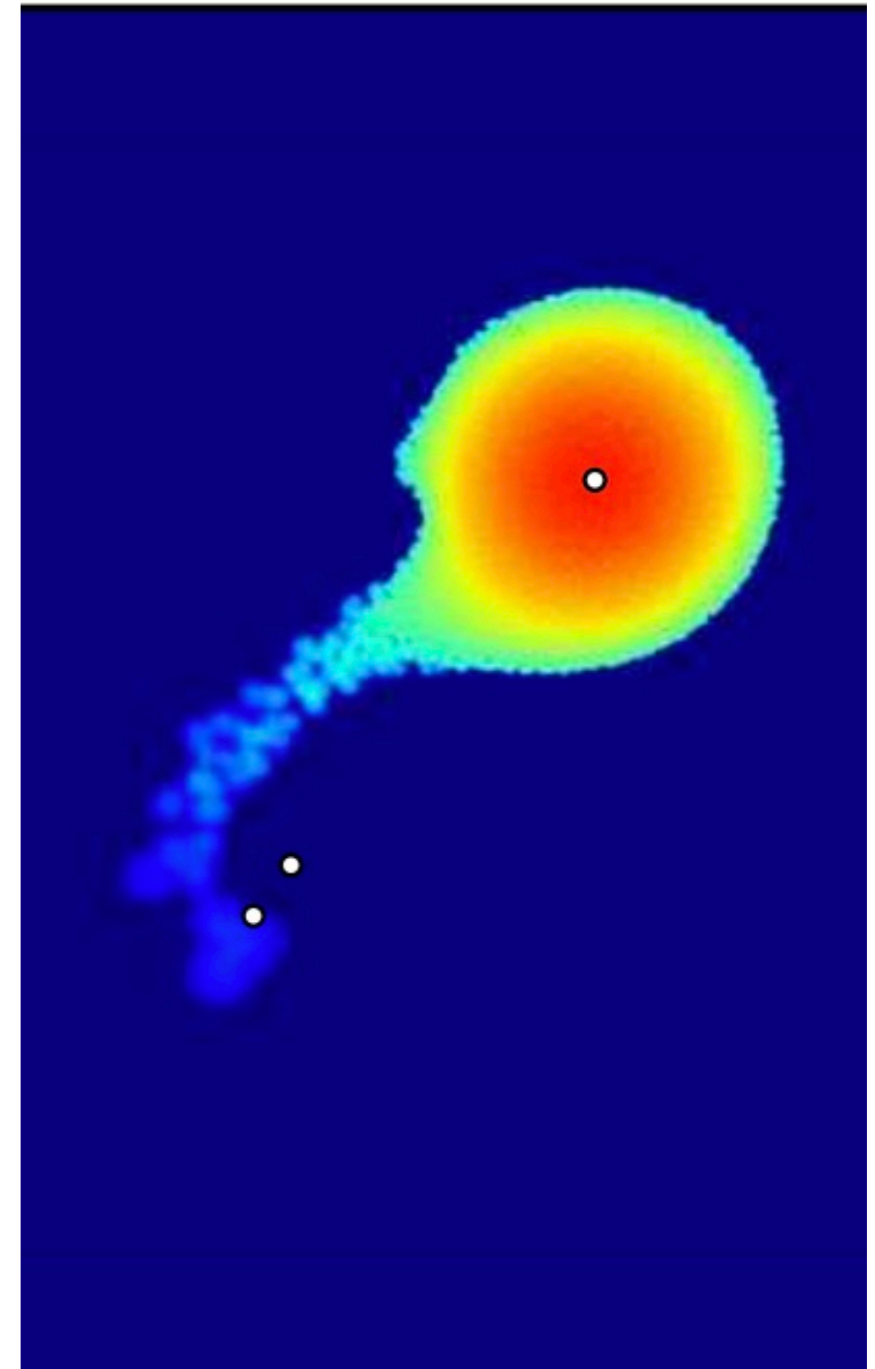
See also: Gao+ '18, Comerford+ '19, DiStefano+ '20, Glanz+ '21

Tertiary donates mass

Formation of barium stars

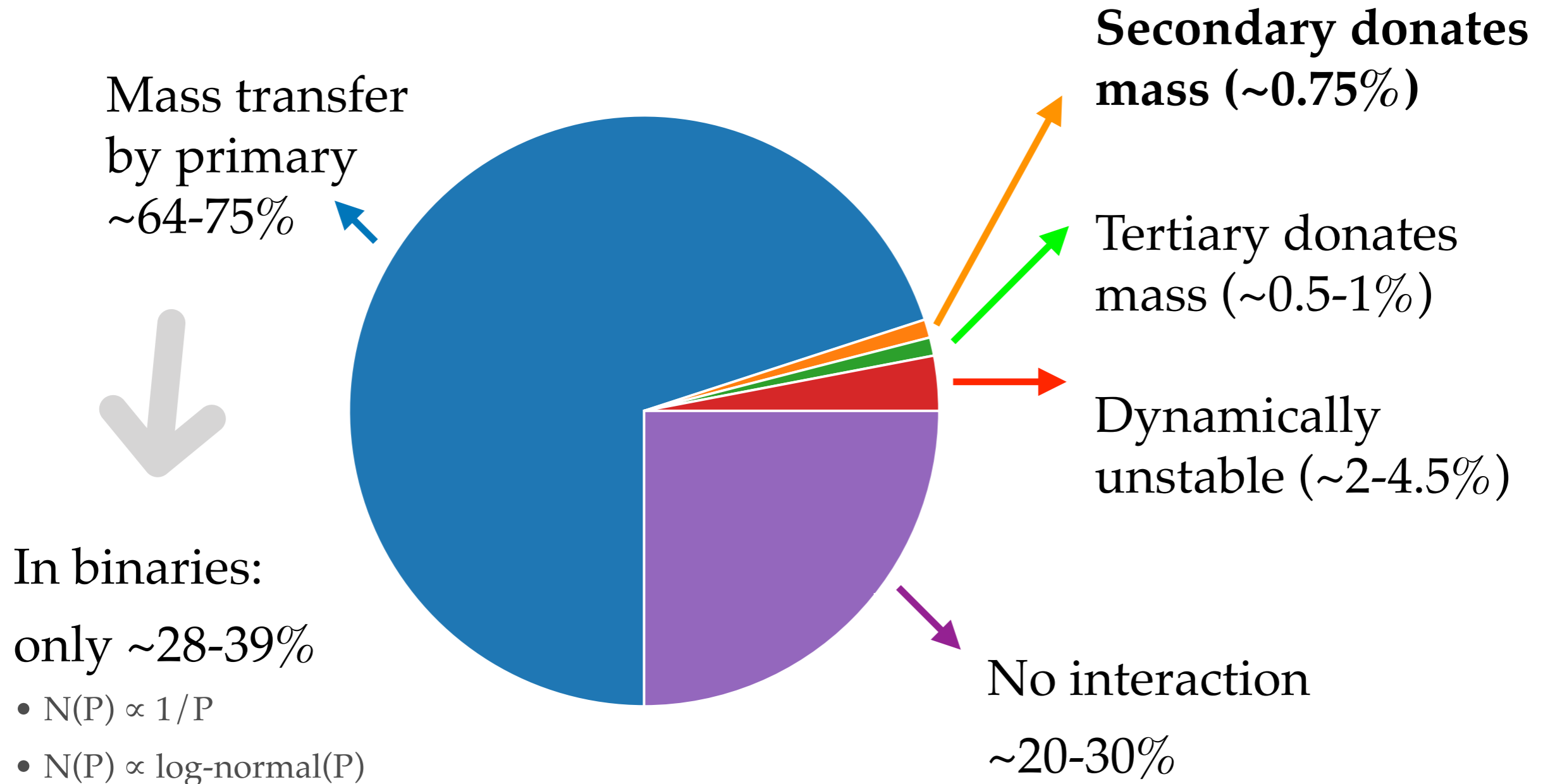
(Gao, Toonen, Leigh 2023)

- ❖ Direct impact accretion onto inner binary leads to orbital shrinkage, eventually merger (De Vries+ '14)
- ❖ Tertiary donor in triples is typically an AGB star (~75-90%, Toonen+ '20)
- ❖ Mass transfer more likely stable because commonly $M_1, M_2 < M_3 < M_1 + M_2$
- ❖ Eccentric orbits of barium stars explained by eccentric mass transfer?



Typical evolution of triples

- low & intermediate mass primaries ($1-7.5M_{\odot}$)



Typical evolution of triples

- low & intermediate mass primaries ($1-7.5M_{\odot}$)

Formation of low-mass X-ray binaries,
cataclysmic variables
- without CE evolution!

Confronting the paradigm of CV
formation (Knigge, Toonen, Boekholt +22)

- $N(P) \propto 1/P$
- $N(P) \propto \log\text{-normal}(P)$

Secondary donates
mass ($\sim 0.75\%$)

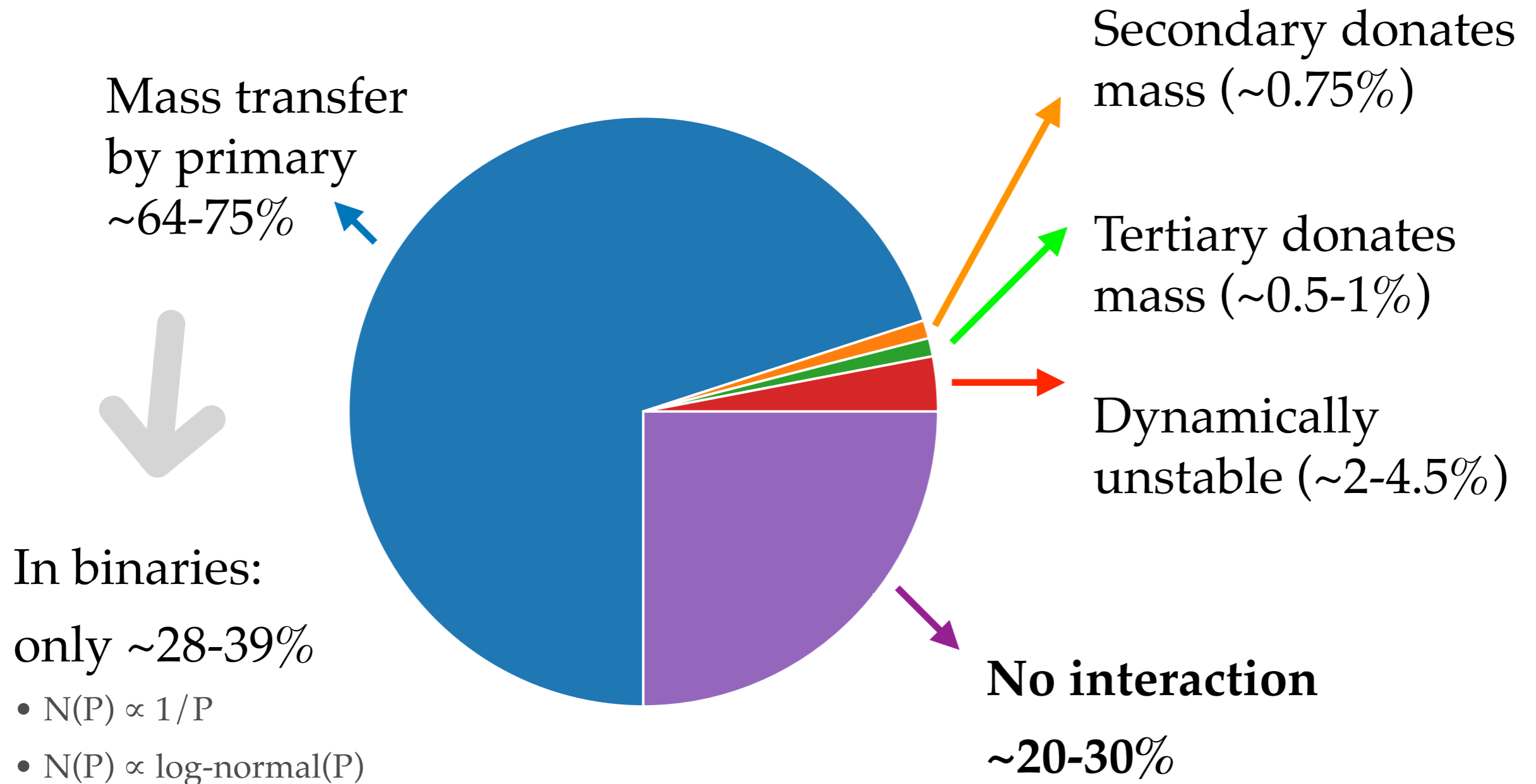
Tertiary donates
mass ($\sim 0.5-1\%$)

Dynamically
unstable ($\sim 2-4.5\%$)

No interaction
 $\sim 20-30\%$

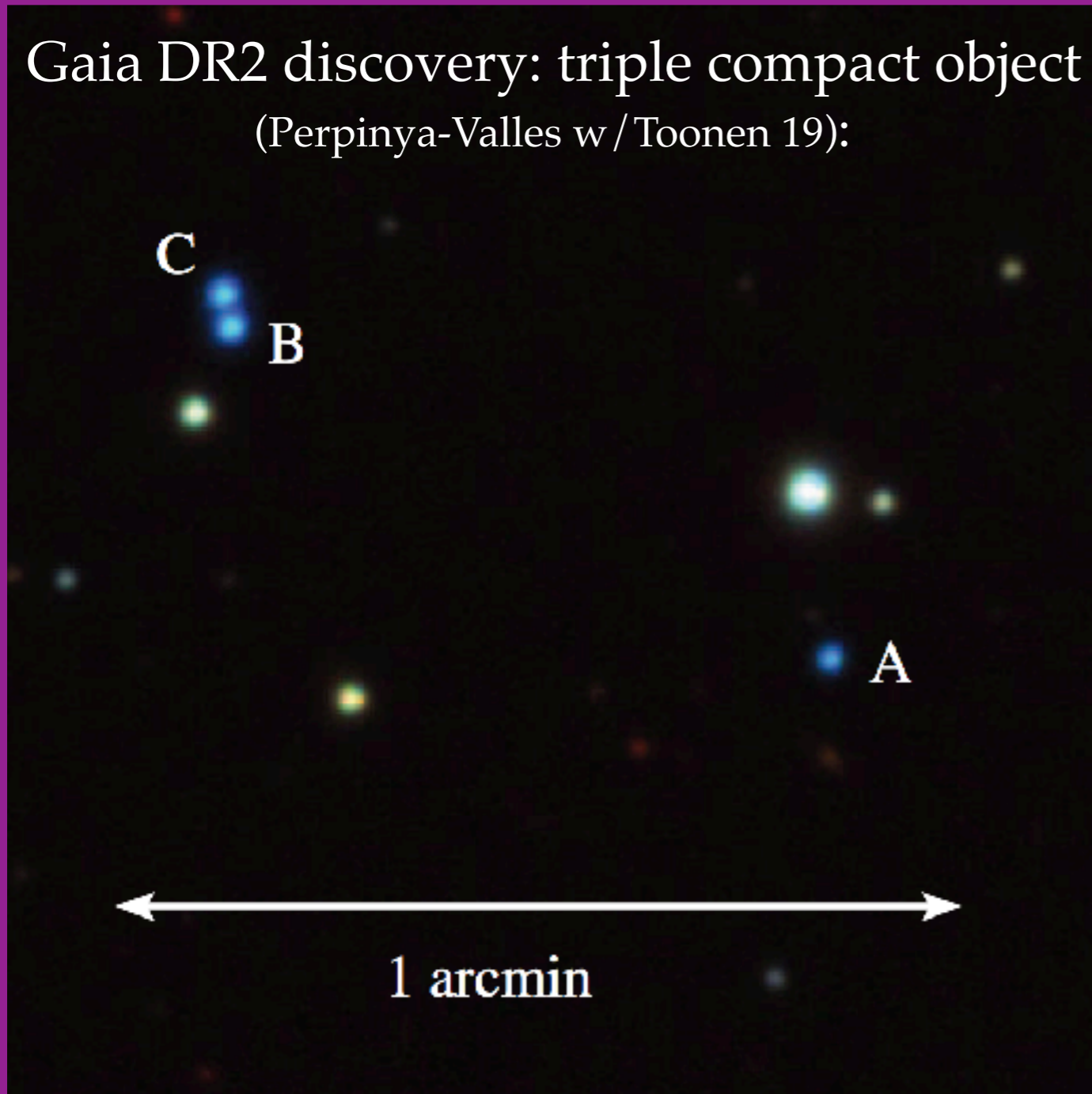
Typical evolution of triples

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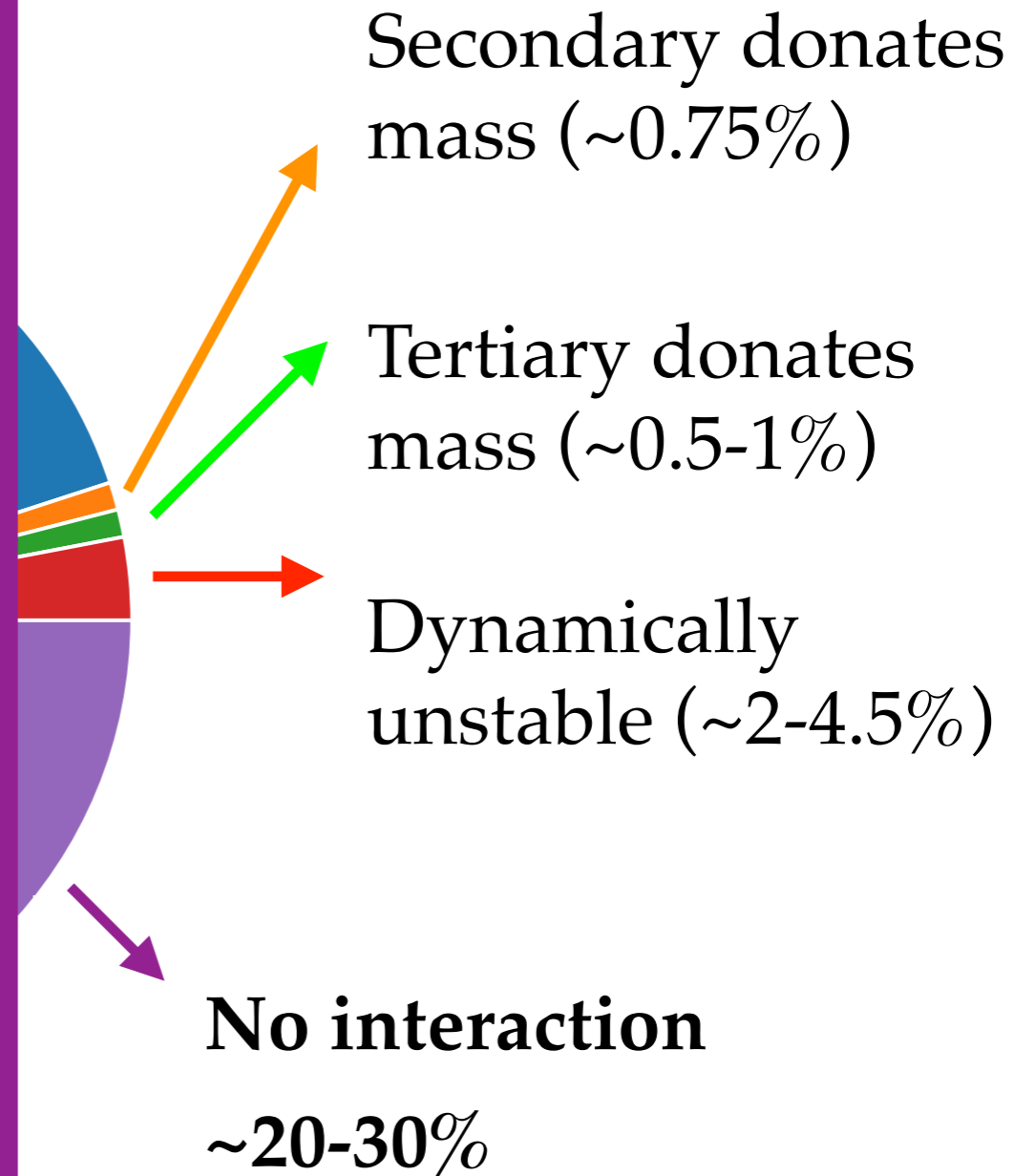


Typical evolution of triples

Gaia DR2 discovery: triple compact object
(Perpinya-Valles w/ Toonen 19):

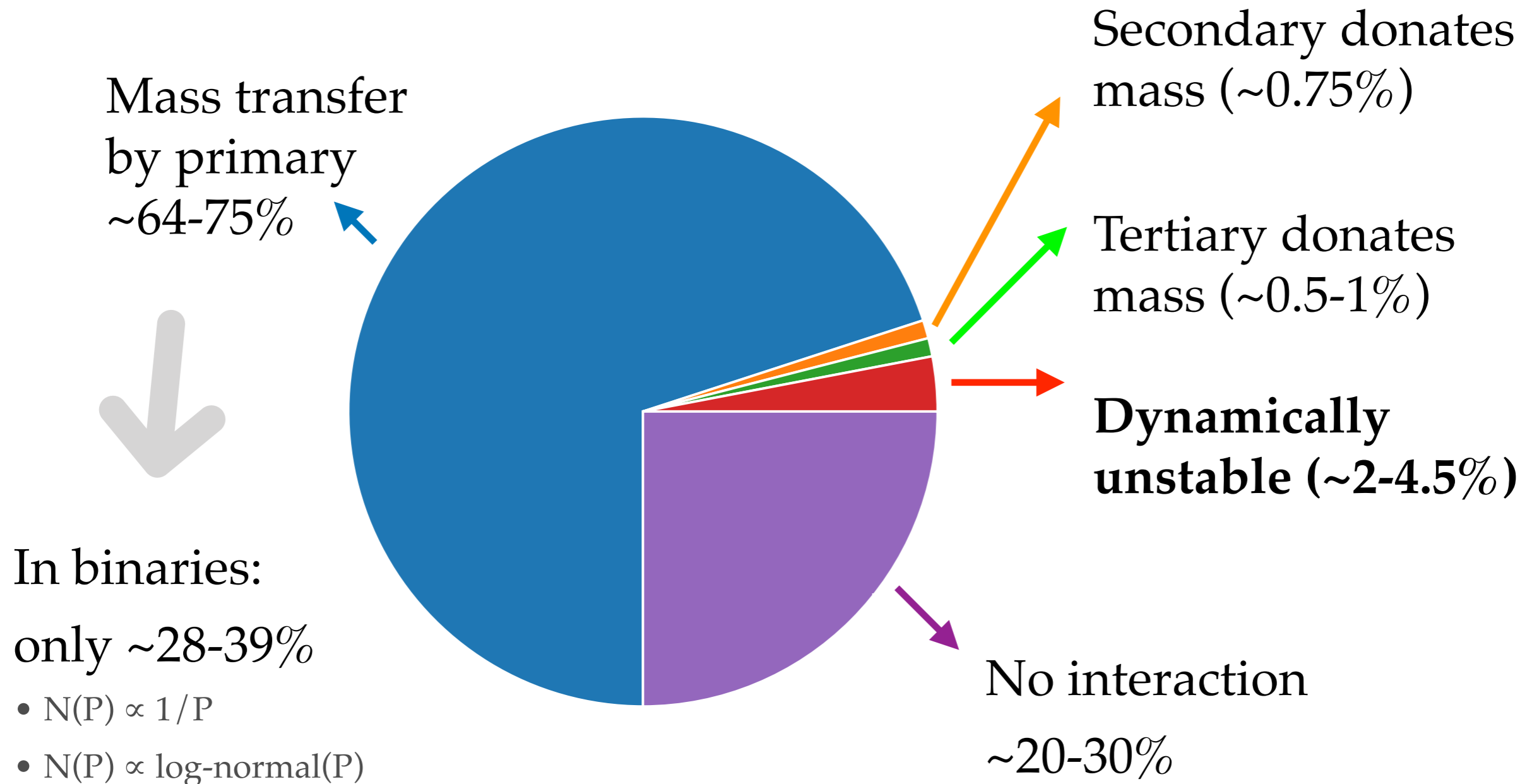


(1-7.5 M_{\odot})



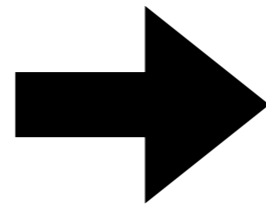
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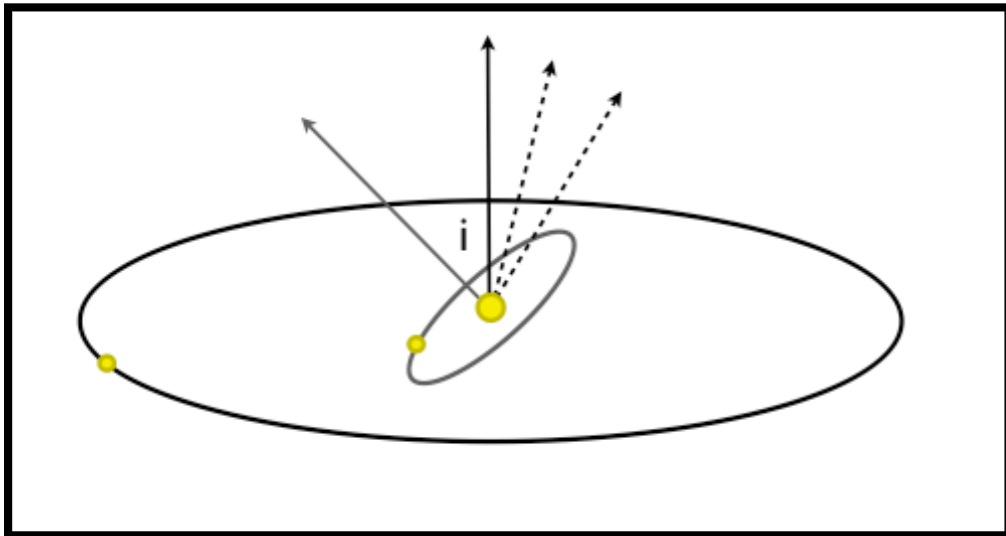


Dynamically unstable triples

Evolution: from secular

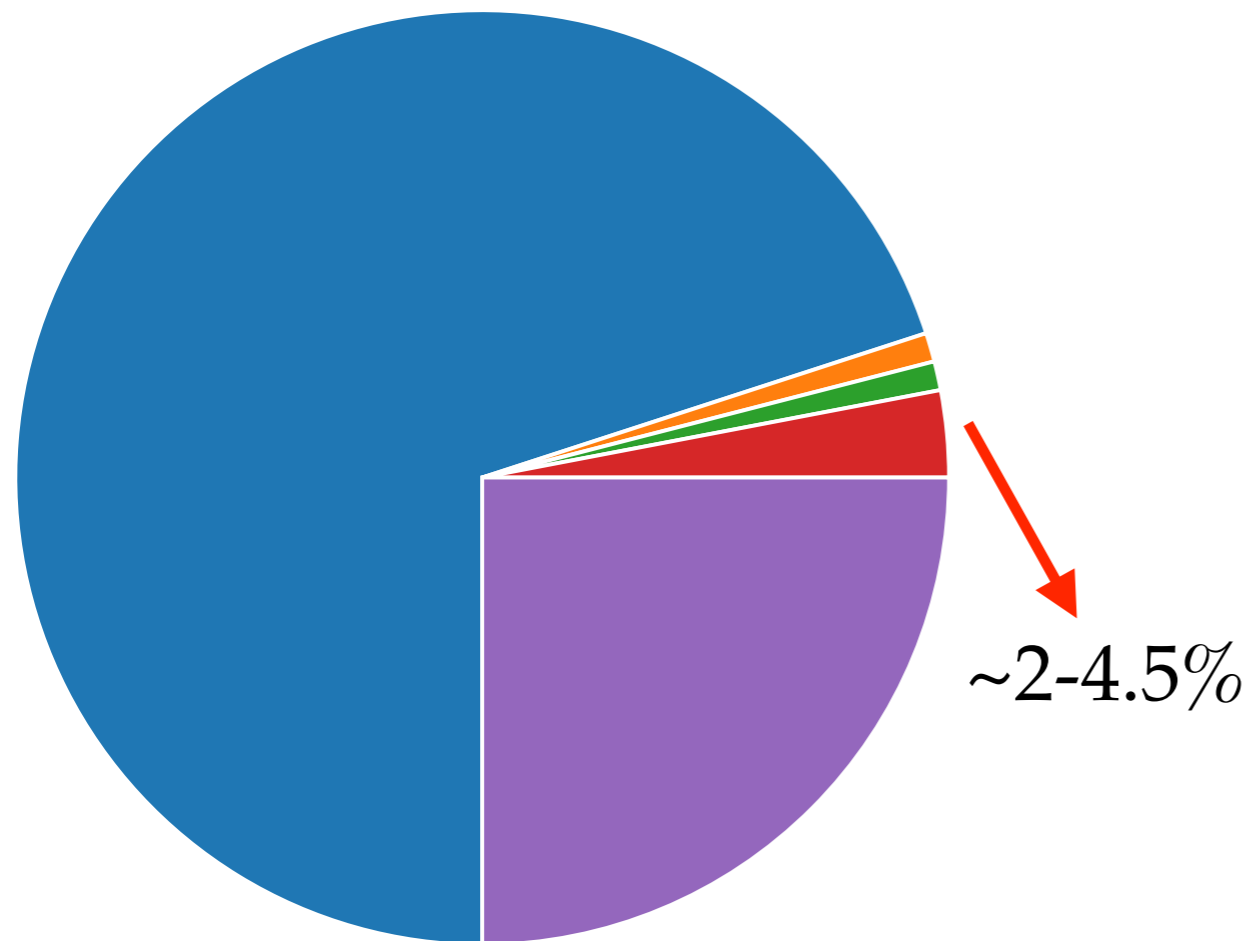


to dynamical timescale



Dynamically unstable triples

➔ Dynamical instability (e.g. Kiseleva+ '94, Iben & Tutukov '99, Toonen+'20 ~1-2 per kyr)



Outcomes

Toonen, Boekholt & Portegies Zwart 2022

- ❖ Ejections (50-70%)
 - ❖ Velocities up to several 10km/s
 - ❖ Origin of runaway stars?
- ❖ Collisions (10-25%)
 - ❖ MW rate of ~0.1 per kyr (consistent with Perets & Kratter '12, Hamers+ '22)
- ❖ Remain on the edge (10-20%)

Triples with compact objects

Collisions of white dwarfs

- ❖ Collision rate $\sim 5e-4 - 2e-2$ per 10000 Msun (Toonen+ '17)
- ❖ Rates enhanced by fly by's (~ 1.5) or WD kicks (~ 2) (Michaely & Perets '15, Hamers & Thompson '19, Michaely '21)



Supernova Type Ia

(Benz+ 89, Katz & Dong '12, Kushnir+ 13):



- ❖ Observed rate: 11.3 ± 2.4 per 10000 Msun (Maoz & Graur '17, Maoz '10, 12)

May lead to more compact objects

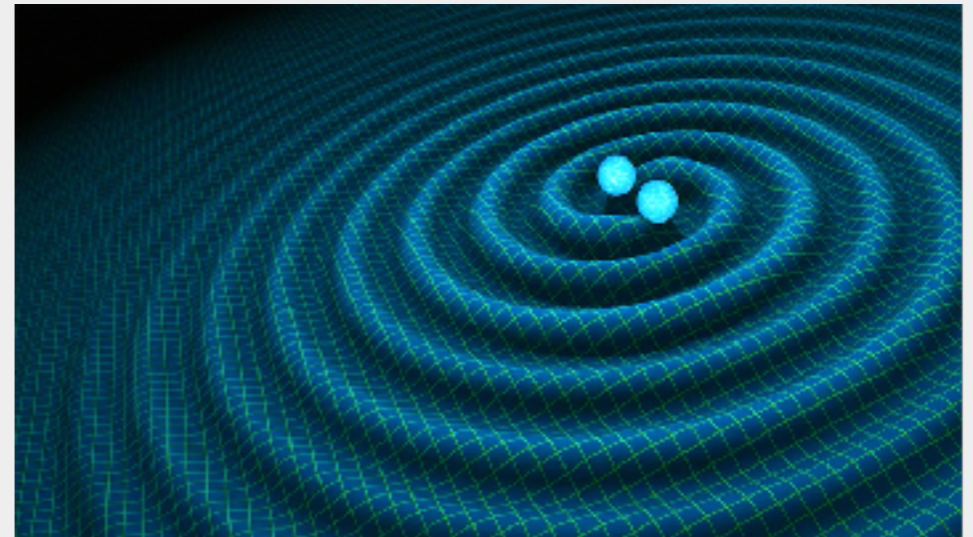
Triples with compact objects

Mergers of black holes



- ❖ Merger rate $\sim 0.4-6 / \text{yr} / \text{Gpc}^3$
(Silsbee & Tremaine '17, Antonini, Toonen, Hamers+ 17, Fragione & Kocsis '20, Martinez+ ' 22)
- ❖ @ low metallicity $\sim 2-25 / \text{yr} / \text{Gpc}^3$ (Rodriguez & Antonini '18)

Gravitational wave sources



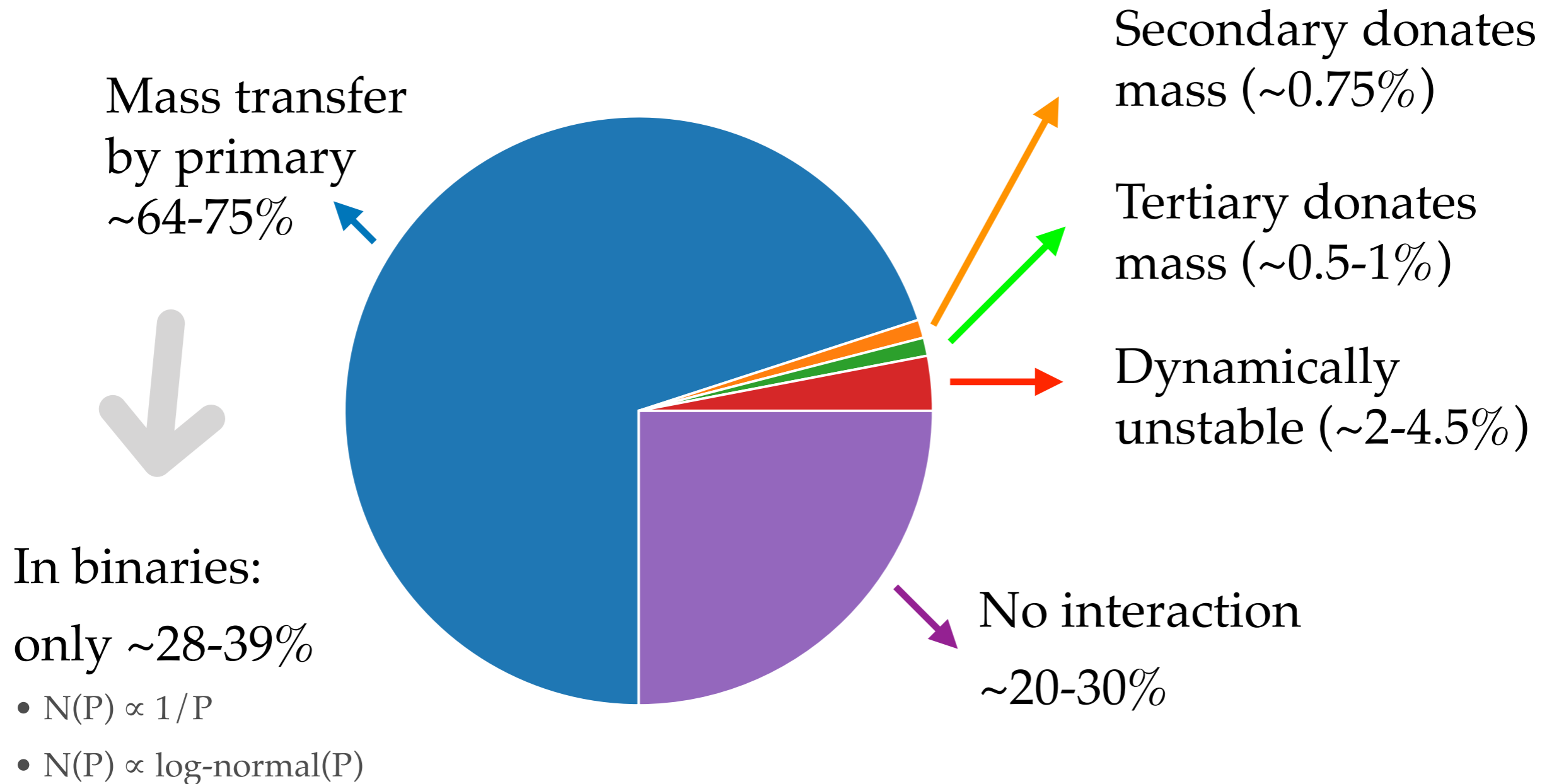
- ❖ Observed rate: LIGO O1-3a:
 $\sim 23.9 (+14.9, -8.6) / \text{yr} / \text{Gpc}^3$
(LSC 20)

May lead
more co
eventua

➔ for NS mergers, see Hamers & Thompson 2019, Fragione & Loeb 2019 (2x)

Typical evolution of triples

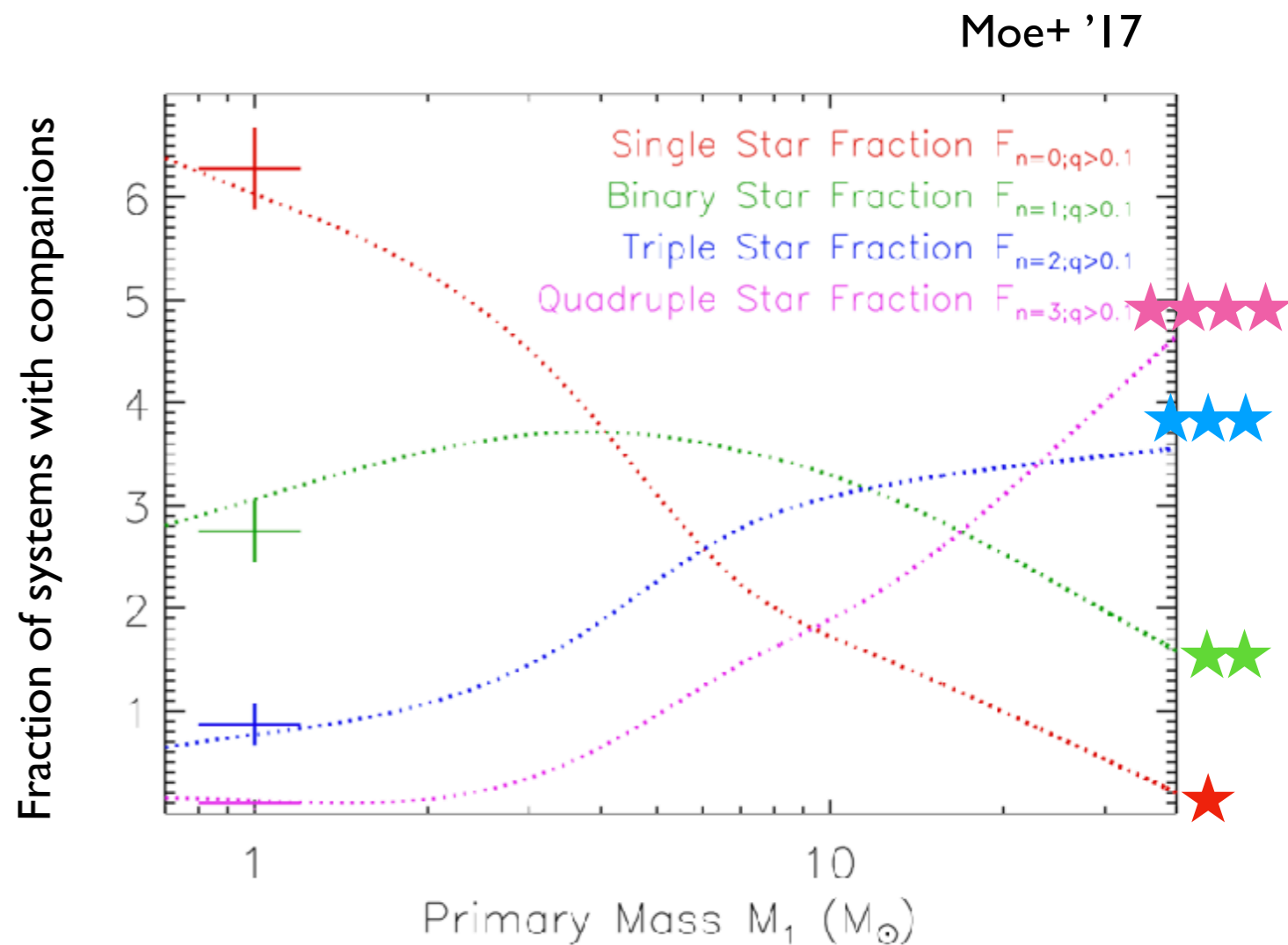
- low & intermediate mass primaries ($1-7.5M_{\odot}$)



Summary

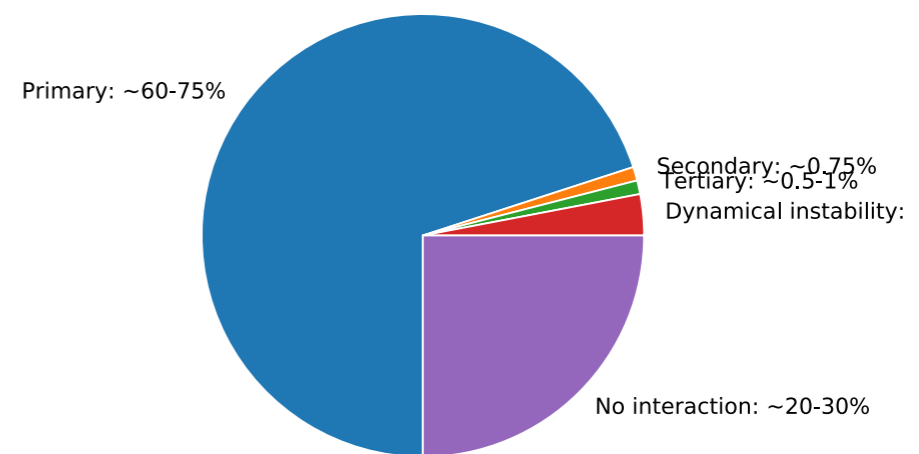
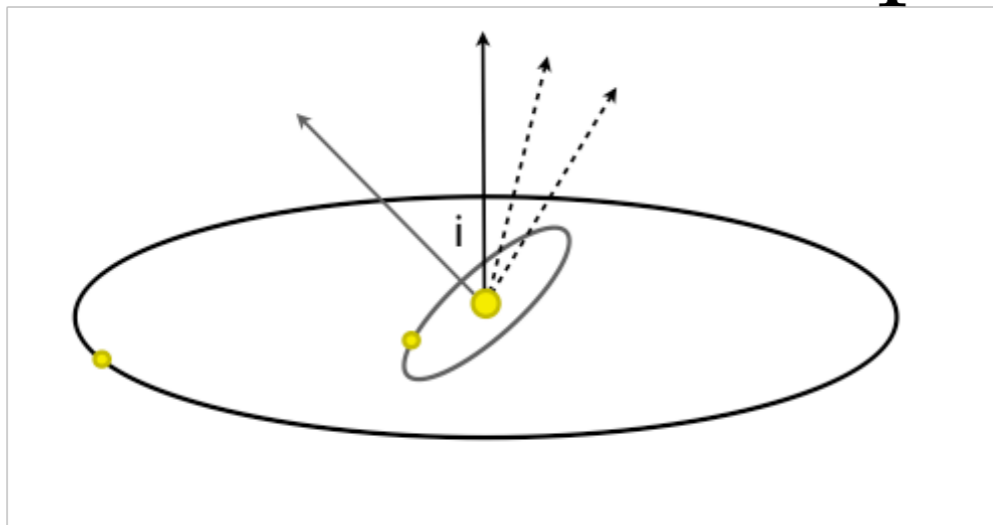
Stellar interactions & transients

- ❖ Future is bright!
 - ❖ Gaia, SDSS, LSST, ZTF, Panstars,
 - ❖ LIGO, LISA etc etc
- ❖ Binaries & triple are abundant
 - ❖ Even dominating for massive stars



Summary

Triple evolution



- ❖ Triples are abundant
- ❖ Public code TRES to simulate triple evolution consistently (Toonen+ '16)
- ❖ Enhanced occurrence rate of mass transfer (Toonen+ '20)
 - ❖ Triples on even footing compared to binary
- ❖ Novel channels: e.g. compact binaries without common-envelope evolution, tertiary mass transfer etc

Summary

Triple evolution major (or even dominant) player for:

- ❖ **Gravitational wave sources** (Silsbee & Tremaine '17, Antonini, Toonen, Hamers+ 17, Fragione & Kocsis '20, Martinez+ ' 22)
- ❖ **Stellar collisions in the field** (Toonen, Boekholt, Portegies Zwart 2022)
- ❖ **Formation of cataclysmic variables**
 - ❖ **Eccentricity from triple evolution to kickstart the enhanced mass transfer rates observed** (Knigge, Toonen, Boekholt 2022)
- ❖ **Elegant formation channel for barium stars** (Gao, Toonen, Leigh 2023)

Checkout:

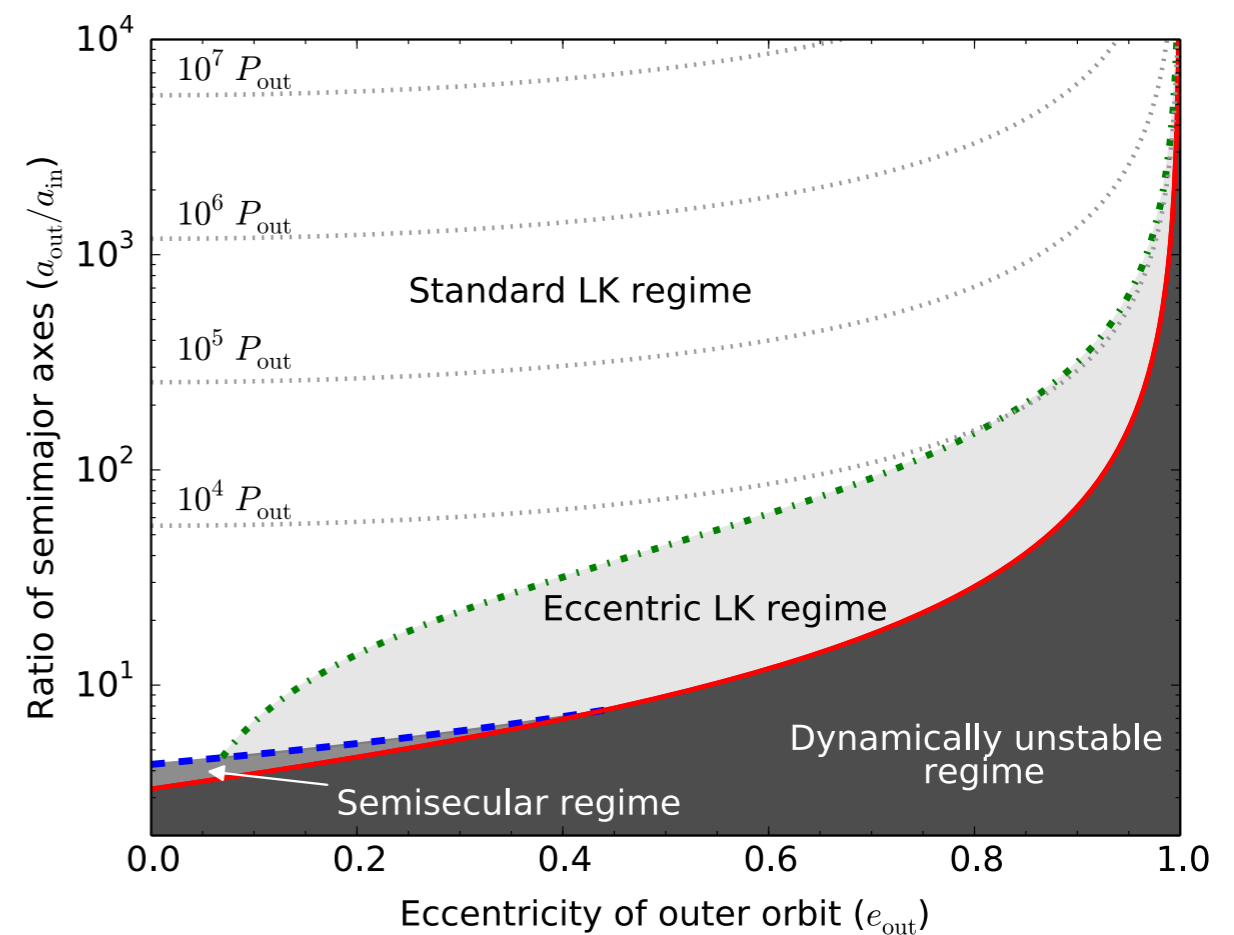
- ❖ Facebook group: triple evolution & dynamics

- ❖ Webinterface:

- ❖ <https://bndr.it/wr64f>
- ❖ when you find a triple... plug it into this Jupyter notebook to asses its dynamics

- ❖ Or find the links on my website:

- ❖ staff.fnwi.uva.nl/s.g.m.toonen



Summary

